

# Higher Heating Value Prediction Model From Proximate And Ultimate Analysis Data

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**Abstract**—This study undertook the formulation of higher heating value (HHV) prediction model from 170 different biomass samples with about one-third being of African-origin. The data were collected from our previous studies and other open literature and subsequently subjected to a multivariable regression analysis technique. The model performance for this study was done in comparison to correlations obtained in the past with the aid of some statistical tools namely average absolute error (AAE) and average bias error (ABE). The models from this study with relatively higher accuracies are  $0.2351 \cdot VM - 0.0775 \cdot ash$  and  $0.3399 \cdot C + 0.3590 \cdot H$  respectively, for proximate and ultimate analyses. They both have AAE values less than 8%. It is noteworthy that the empirical relation for proximate analysis would be of profound utility within the African context giving the associated technical constraints in HHV determination.

**Keywords**— Higher heating value; biomass; proximate; ultimate; multivariable regression

## I. INTRODUCTION

In recent decades, there has arisen a grave global concern regarding the dwindling fossil fuel reserves, and the adverse environmental consequences, primarily, climate change and global warming phenomena, engendered by its utilization. In a bid to combat this challenge, biomass resource has been identified as an attractive renewable energy resource. It is the fourth most abundant primary energy source, after the conventional ones, namely, petroleum, coal, and natural gas [1]. Biomass materials are readily available at relatively cheaper prices – often as concomitant by-products of agro-industrial activities, constituting waste management and disposal challenges [2]. Another major merit is the fact that the utilization of biomass for thermal energy generation is

carbon neutral as well as low in SO<sub>x</sub> and NO<sub>x</sub> emissions.

Typically, lignocellulosic biomass is used as a feedstock material for heating and electricity generation, biofuels production, and bioenergy applications. The design and simulation of efficient combustion and reaction systems require fundamental data of biomass physical and chemical characteristics alongside their calorific value. This value is the measure of heat energy liberated per unit mass of fuel during its complete combustion and it is expressed as either higher heating value (HHV) or lower heating value (LHV). The former accounts for the total enthalpy that includes the latent heat of vaporization of water, while the LHV excludes the latent heat. The calorific value determination can be undertaken experimentally with the aid of an adiabatic bomb calorimeter. However, this equipment and its operation could be expensive, time-consuming, and/or require some expertise, which in some instances may not be readily available [3], [4]. This necessitates the formulation of reliable empirical models that utilize data from relatively simple experiments. Hitherto, several HHV prediction correlations have been formulated based on characterization data from different organic materials, ranging from fossil fuels, mostly coal, to a vast array of biomass residues cutting across diverse regional locations [5]–[8].

One of the earliest model is the Dulong's linear relation for the estimation of coal's HHV; however, regarding biomass applications, it is severely limited [3]. Though there are more recent prediction models derived from biomass data, some of them are fraught with a number of imprecisions [7]–[9]. For instance, Vargas-moreno [3] opined that the inclusion of inter-related variables such as fixed carbon [FC] as an independent variable is mathematically questionable because it is usually estimated as a difference between 100% and the sum of the other elements (Volatile matter [VM], and ash [ash]) on a dry-basis. A similar argument could be made for the inclusion of elemental oxygen [O] from elemental analysis for the development of HHV prediction models. Furthermore,

some authors fail to state categorically the basis on which their data is being reported [3]. In terms of regional spread, most of the regression models have been developed from biomass data obtained in Europe and Asia with little focus on biomass resources emanating from [1], [10]. Garcia et al [7] worked on biomass of Spanish origin and through multivariable regression analysis (MVRA) proposed four correlation equations. Similarly, Thipkhunthod et al [6] and Chang et al [11] respectively derived regression models from Thailand-based and Taiwan-based biomass materials. Even in instances of a wider geographical reach, information on biomass originating from Africa are virtually absent. This is clearly demonstrated in a recent publication [1]. According to Azeez et al [12], variation in the elemental constituent of an African hardwood species relative to a counterpart European species, significantly influenced the outcome of a pretreatment process. The dependence of biomass characteristics on geographical location, climatic condition and management practices has also been underscored in literature [13]. To the best of the authors' knowledge, this is a first attempt to include a sizeable amount (more than 30%) of characterization data gathered from biomass of African origin.

The aim of this research was to formulate an HHV prediction models from proximate and ultimate analysis data using an MVRA technique. The study also compared the predictive accuracy of the model from this study with selected ones.

## II. MATERIALS AND METHODS

### A. Data Collection

A database of proximate, ultimate analyses and HHV on 170 biomass samples was obtained from our previous study [14] and other published literature as presented in Table 1. Specifically, the data gathering was restricted to articles published not later than 2010 and they were reported on a dry-basis and dry-ash-free basis [13]. The data were also from those in which the countries of origin of the sample source were explicitly stated and experimental HHV measurements taken. To ensure consistency in terms of the basis of experimental reporting, those reported otherwise, were converted into dry-basis (db) and dry-ash-free (daf) basis for proximate and ultimate analysis data respectively. The data on chlorine, where present, were ignored. Furthermore, a subset of 136 samples was selected randomly for the model development, while the remaining data sets were incorporated for model validation.

The samples under consideration cover a vast variety of lignocellulosic biomass that may be broadly grouped into four categories namely (i) herbaceous and agricultural residues (HAR), (ii) herbaceous and agricultural grasses (HAG), (iii) herbaceous and agricultural straws (HAS), and (iv) wood and woody biomasses (WWB) (Vassilev et al. 2010). Table 1 shows that volatile matter (VM) and ash contents respectively varied from 59.2 to 95.5% and 0.1 to 27%, while C, H, N, and S contents varied from 24.51 to 59.23%, 0.27 to 11.28%, 0.07 to 8.03%, and 0 to 3.19%. The HHV ranged from 12.83 to 27.63 MJ/kg.

Table 1 Proximate, ultimate analyses and HHV data from published literature

| Biomass residues                           | Proximate Analysis |           |                       | Ultimate Analysis |       |       |       |                    | HHV <sub>exp</sub><br>(MJ/kg) | Country of Origin | Ref  |
|--|--------------------|-----------|-----------------------|-------------------|-------|-------|-------|--------------------|-------------------------------|-------------------|------|
|  | VM (wt%)           | Ash (wt%) | FC <sup>a</sup> (wt%) | C (%)             | H (%) | N (%) | S (%) | O <sup>a</sup> (%) |                               |                   |      |
| Herbaceous and Agricultural Residues (HAR) |                    |           |                       |                   |       |       |       |                    |                               |                   |      |
| Palm stem                                  | 81.2               | 3.5       | 15.3                  | 49.23             | 6.11  | 0.29  | 0.13  | 44.05              | 17.38                         |                   |      |
| Palm branch                                | 79.6               | 7.8       | 12.6                  | 49.47             | 6.08  | 0.21  | 0.17  | 42.63              | 16.24                         |                   |      |
| Palm fiber                                 | 79.0               | 11.8      | 9.3                   | 59.23             | 8.06  | 0.79  | 0.08  | 31.77              | 21.98                         |                   |      |
| Coffee husks                               | 83.2               | 2.5       | 14.3                  | 50.61             | 6.25  | 0.83  | 0.07  | 42.21              | 18.34                         |                   |      |
| Masai Cashew nuts                          | 84.1               | 1.9       | 14                    | 57.07             | 7.03  | 0.45  | 0.05  | 35.36              | 22.38                         |                   |      |
| Olam Cashew nuts                           | 84.8               | 2         | 13.1                  | 58.05             | 7.14  | 0.46  | 0.04  | 34.28              | 22.83                         |                   |      |
| Rice husks*                                | 59.2               | 26.2      | 14.6                  | 48.25             | 6.1   | 0.26  | 0.03  | 45.26              | 13.24                         |                   |      |
| Rice bran*                                 | 64.6               | 21.1      | 14.2                  | 47.91             | 6.34  | 0.7   | 0.06  | 44.87              | 13.93                         |                   |      |
| Sugarcane bagasse                          | 80.5               | 3.3       | 16.2                  | 49.77             | 6.11  | 0.16  | 0.02  | 43.87              | 17.33                         |                   |      |
| Sisal leaf                                 | 80.2               | 7.2       | 12.6                  | 50.64             | 6.14  | 0.15  | 0.03  | 42.99              | 17.23                         |                   |      |
| Sisal bole                                 | 84.1               | 3.1       | 12.8                  | 49.54             | 6.19  | 0.1   | 0.03  | 44.07              | 17.2                          |                   |      |
| Sisal pole                                 | 79.3               | 6.1       | 14.6                  | 50.03             | 6.39  | 1.77  | 0.14  | 41.62              | 17.35                         |                   |      |
| Cocoa pod                                  | 76.3               | 12        | 11.6                  | 43.87             | 5.82  | 2.23  | 0.57  | 47.28              | 17.08                         | Nigeria           | [16] |
| Cocoa pod                                  | 66.08              | 14.9      | 19                    | 50.28             | 6.69  | 0.19  | 0.19  | 42.64              | 18.1                          | Colombia          | [17] |
| Corncob                                    | 88.4               | 3.2       | 8.3                   | 43.3              | 6     | 0.93  | -     | 49.37              | 16.99                         | Ghana             |      |
| Rice husks*                                | 63.7               | 27        | 9.3                   | 34.9              | 5.15  | 0.31  | 0.64  | 59                 | 14.08                         | Ghana             |      |
| Sugarcane bagasse                          | 86.8               | 4.3       | 8.9                   | 44.31             | 5.73  | 0.63  | -     | 49.11              | 16.88                         | Ghana             | [16] |
| Jatropha cakes                             | 80.6               | 7.2       | 12.2                  | 44.42             | 6.23  | 4.33  | 0.51  | 44.51              | 21.24                         | Nigeria           |      |
| Parinari fruit shell                       | 80.3               | 4.8       | 14.9                  | 48.04             | 5.76  | 2.13  | 0.1   | 43.53              | 20.47                         | Nigeria           |      |
| Corncob                                    | 80.2               | 3.1       | 16.7                  | 49                | 6     | 0.3   | 0.08  | 44.7               | 17.2                          | South Africa      |      |
| Sugarcane bagasse                          | 76.9               | 5.3       | 17.8                  | 50.3              | 6.3   | 0.3   | 0.07  | 43.1               | 17.5                          | South Africa      | [18] |
| <i>Moringa peregrina</i> seed husk         | 78.9               | 2.5       | 18.6                  | 45.42             | 6.34  | 0.94  | 0.57  | 46.73              | 18.21                         | Sudan             | [19] |
| Jatropha seed husk                         | 64.9               | 3.9       | 31.1                  | 50.9              | 5.8   | 0.8   | 0.08  | 39.5               | 17.98                         | India             | [20] |
| <i>Moringa peregrina</i> seed oil cake     | 80.3               | 4.1       | 15.6                  | 46.42             | 7.76  | 8.03  | 3.19  | 36.6               | 20.65                         | Sudan             | [19] |
| Sweet sorghum bagasse                      | 79.2               | 4.6       | 16.2                  | 43.5              | 5.6   | 0.28  | 0.13  | 50.5               | 17.3                          | South Africa      | [21] |
| Almond shell                               | 82                 | 2.2       | 15.8                  | 46.35             | 5.67  | 0.3   | 0.22  | 47.2               | 18.28                         |                   |      |
| Olive stone                                | 78.3               | 1.4       | 20.35                 | 46.55             | 6.33  | 1.81  | 0.11  | 45.2               | 17.88                         |                   |      |
| Pine kernel shell                          | 77.6               | 2.7       | 19.7                  | 47.91             | 4.9   | 0.31  | 0.6   | 46.28              | 18.89                         |                   |      |
| Chestnut shell                             | 67                 | 3.9       | 29                    | 42.31             | 5.17  | 0.42  | 0.33  | 51.77              | 14.31                         |                   |      |
| Areca nut husk                             | 80.6               | 2.5       | 16.9                  | 48.8              | 5.79  | 1.95  | 0.1   | 43.45              | 18.21                         |                   |      |
| Coconut shell                              | 79.2               | 1.4       | 19.4                  | 47.93             | 6.05  | 0.15  | 0.24  | 45.63              | 18.88                         |                   |      |
| Coffee husks                               | 76.2               | 5.8       | 18                    | 45.06             | 6.42  | 2.53  | 0.48  | 45.51              | 18.33                         |                   |      |
| Corncob                                    | 83                 | 2.4       | 14.6                  | 44.78             | 6.02  | 0.22  | 0.21  | 48.77              | 17.69                         |                   |      |
| Hazelnut shell                             | 77                 | 2.2       | 20.8                  | 47.8              | 6.14  | 0.27  | 0.16  | 45.64              | 18.87                         |                   |      |
| Pea husk                                   | 83                 | 4.5       | 12.5                  | 24.51             | 0.27  | 0.42  | 1     | 73.8               | 15.46                         |                   |      |
| Peanut shell                               | 81                 | 2.5       | 16.5                  | 49.35             | 6.4   | 1.05  | 0.24  | 42.96              | 20.01                         |                   |      |
| Pistachio shell                            | 82.5               | 1.3       | 16.2                  | 44.69             | 5.16  | 0.11  | 0.18  | 49.87              | 16.2                          |                   |      |
| Rice husks*                                | 73                 | 13.7      | 13.3                  | 26.69             | 2.88  | 0.21  | 0.17  | 70.05              | 15.9                          |                   |      |
| Walnut shell                               | 79                 | 2.3       | 18.7                  | 46.97             | 6.27  | 0.22  | 0.1   | 46.44              | 18.38                         |                   |      |
| Banana peel                                | 73                 | 4.5       | 22.5                  | 50.4              | 6.3   | 2.56  | 0.39  | 40.4               | 18.87                         | China             | [23] |
| Durian shell                               | 73.9               | 3.3       | 22.8                  | 40.98             | 4.44  | 1.31  | 0.34  | 52.93              | 13.79                         | Malaysia          | [24] |
| Coffee tree leaves                         | 74.71              | 7.17      | 18.12                 | 53.97             | 6.55  | 3.54  | 0.43  | 35.5               | 19.45                         | Brazil            | [25] |
| Coffee parchment                           | 74.07              | 5.84      | 20.09                 | 50.69             | 6.23  | 0.82  | 0.2   | 42.05              | 18.3                          | Brazil            | [25] |
| Sugarcane bagasse                          | 81.86              | 2.04      | 15.98                 | 42.09             | 5.42  | 0.18  | 0.12  | 51.5               | 16.79                         | Colombia          | [26] |
| Corn stover                                | 82.13              | 5.01      | 12.86                 | 56.08             | 5.97  | 0.65  | 0.11  | 37.19              | 18.78                         | USA               | [27] |
| Beer bagasse                               | 79                 | 3         | 18                    | 50.13             | 7.16  | 3.58  | 0.25  | 38.88              | 21                            | Spain             | [28] |
| Orange Juice residues                      | 76                 | 6         | 18                    | 46.78             | 6.38  | 1.06  | 0.05  | 45.72              | 17                            | Spain             | [28] |
| Adzuki bean waste                          | 76.1               | 6.24      | 17.66                 | 39.41             | 10.68 | 2.95  | 0.93  | 46.03              | 19.85                         | Malaysia          | [29] |
| Oil palm empty fruit bunch                 | 81.53              | 6.28      | 12.19                 | 45.23             | 6     | 1.21  | 0.13  | 47.43              | 17.57                         | Malaysia          | [30] |
| Oil palm trunk                             | 77.1               | 18.6      | 4.29                  | 50.1              | 7.59  | 1.04  | 0.11  | 41.2               | 14.5                          | Malaysia          | [31] |
| Seed cake (jatropha)                       | 68.63              | 5.28      | 26.08                 | 46.15             | 6.47  | 4.48  | 0.2   | 42.71              | 19.28                         | Botswana          |      |
| Jatropha stem                              | 70.68              | 7.94      | 21.39                 | 43.68             | 6.32  | 1.33  | 0.21  | 48.46              | 18.39                         | Botswana          | [32] |
| Jatropha fruit husk                        | 61.51              | 19.74     | 18.75                 | 36.05             | 5.37  | 1.07  | 0.37  | 57.15              | 13.57                         | Botswana          |      |
| Empty fruit bunch                          | 86.93              | 3.63      | 9.44                  | 46.62             | 6.45  | 1.21  | 0.035 | 45.66              | 17.02                         | Malaysia          | [33] |
| Empty fruit bunches                        | 77.99              | 4.98      | 17.04                 | 40.93             | 5.42  | 1.56  | 0.31  | 51.78              | 16.8                          | Malaysia          |      |
| Palm kernel shell                          | 69.2               | 10.5      | 16                    | 41.33             | 4.57  | 0.99  | 0.09  | 53.02              | 16.3                          | Malaysia          | [34] |
| Palm mesocarp fiber                        | 73.04              | 10.83     | 16.14                 | 43.19             | 5.24  | 1.59  | 0.19  | 49.79              | 19                            | Malaysia          |      |
| Palm kernel shell                          | 77.5               | 2.2       | 20.3                  | 56.1              | 5.9   | 0.4   | 0.03  | 37.6               | 16.3                          | Malaysia          | [35] |
| Bambara Groundnut                          | 73.83              | 10.1      | 16.08                 | 34.63             | 11.28 | 1.16  | 1     | 51.93              | 19.19                         | Malaysia          | [29] |

|   |       |       |       |       |      |      |      |       |       |              |      |
|---|-------|-------|-------|-------|------|------|------|-------|-------|--------------|------|
| Tobacco waste                           | 62.44 | 20.78 | 16.78 | 46.96 | 5.92 | 3.55 | 0.66 | 42.91 | 13.88 | China        | [36] |
| Mallee residue                          | 77.9  | 2.9   | 19.2  | 52.71 | 6.01 | 0.53 | 0.08 | 40.67 | 20.42 | Australia    | [37] |
| Soybean waste                           | 74.8  | 5     | 20.2  | 43.8  | 6.3  | 1.4  | 0.8  | 48.5  | 18.77 | India        | [38] |
| Almond shell                            | 75.08 | 4.09  | 20.83 | 49.38 | 5.82 | 0.56 | 0.25 | 44    | 18.71 | USA          | [39] |
| Almond hull                             | 71.24 | 8.57  | 20.19 | 49.4  | 6.02 | 1.08 | 0.22 | 43.28 | 17.66 | USA          | [39] |
| Corn cob                                | 79.31 | 7.23  | 13.46 | 41.16 | 5.11 | 0.46 | -    | 53.27 | 16.73 | South Africa | [40] |
| Pine cone                               | 78.62 | 1.54  | 19.85 | 56.47 | 6.55 | 0.37 | -    | 36.61 | 17.45 | Turkey       | [40] |
| Corn stalk                              | 73.3  | 11.7  | 15    | 50.61 | 6.31 | 0.67 | -    | 42.41 | 12.83 | Turkey       | [41] |
| Peanut shell                            | 73.9  | 2.3   | 23.8  | 52.73 | 6.1  | 1.33 | -    | 39.84 | 16.35 | Turkey       | [41] |
| Potato peel                             | 76.5  | 9.3   | 14.2  | 43.8  | 6    | 4.1  | -    | 46.2  | 17.4  | USA          | [42] |
| <i>Indigofera</i> biomass residue       | 87.7  | 10.2  | 2.1   | 49.2  | 7.2  | 2.5  | -    | 41.1  | 17.09 | India        | [43] |
| Soy peel                                | 91.4  | 1.17  | 7.44  | 45.04 | 6.7  | 2.9  | -    | 45.35 | 17.9  | Brazil       | [43] |
| Rice husks                              | 71.24 | 12.5  | 16.27 | 35.86 | 4.4  | 0.28 | -    | 59.46 | 16.35 | Brazil       | [43] |
| Coffee husks                            | 75.4  | 2     | 22.7  | 43.34 | 5.55 | 2.25 | -    | 48.86 | 18.06 | Brazil       | [43] |
| Coconut fibers                          | 77    | 2.96  | 20.05 | 47.4  | 5.41 | 0.55 | -    | 46.64 | 18.7  | Brazil       | [44] |
| Bamboo                                  | 81.08 | 1.71  | 17.2  | 44.6  | 5.55 | 0.91 | -    | 48.93 | 18.33 | Brazil       | [44] |
| Banana stalk                            | 70.86 | 7.76  | 21.41 | 37.95 | 4.73 | 1.46 | -    | 55.85 | 15.73 | Brazil       | [44] |
| Banana stem                             | 81.71 | 8.14  | 10.14 | 39    | 5.44 | 0.82 | -    | 54.84 | 16.13 | Brazil       | [44] |
| <i>Mbwazirume</i> peel                  | 78.29 | 6.52  | 15.19 | 46.94 | 5.79 | 0.23 | 0.3  | 46.74 | 18.28 | Uganda       | [45] |
| <i>Nakyinyika</i> peel                  | 79.86 | 5.44  | 14.7  | 46.22 | 5.6  | 0.41 | 0.36 | 47.41 | 17.76 | Uganda       | [45] |
| Palm kernel shell                       | 76.1  | 2.9   | 21    | 55.2  | 6.4  | 0.45 | -    | 37.95 | 21    | Nigeria      | [46] |
| Rice husk                               | 68.25 | 14.83 | 16.92 | 39.48 | 5.71 | 0.67 | -    | 54.12 | 17.34 | Brunei       | [47] |
| Oil palm frond                          | 82.12 | 11.9  | 5.98  | 37.52 | 6.9  | 3.52 | 0.28 | 51.77 | 14.49 | Malaysia     | [48] |
| Oil palm trunk                          | 85.7  | 8.11  | 6.19  | 38.26 | 8.21 | 0.59 | 0.44 | 52.5  | 16.34 | Malaysia     | [48] |
| Empty fruit bunch                       | 88.71 | 6.98  | 4.32  | 38.26 | 8.21 | 0.59 | 0.44 | 52.5  | 16.07 | Malaysia     | [48] |
| Palm kernel shell                       | 71.84 | 11    | 17.16 | 48.36 | 7.66 | 1.03 | 0.38 | 42.57 | 17.32 | Malaysia     | [48] |
| Rice husk                               | 69.67 | 19.68 | 10.63 | 37.43 | 8.01 | 0.82 | 0.37 | 53.37 | 14.37 | Malaysia     | [48] |
| Kenaf                                   | 86.63 | 6     | 7.36  | 40.71 | 9.38 | 0.32 | 0.47 | 49.12 | 16.66 | Malaysia     | [48] |
| <i>Sorghum bicolor</i> glume            | 78.9  | 7.54  | 13.6  | 42.4  | 5.27 | 0.74 | -    | 51.6  | 16.4  | Nigeria      | [49] |
| Tea waste                               | 72.92 | 5.75  | 21.33 | 48.6  | 5.43 | 2.6  | -    | 43.37 | 27.63 | India        | [50] |
| Herbaceous and Agricultural Straw (HAS) |       |       |       |       |      |      |      |       |       |              |      |
| Rice straw                              | 81.13 | 12.77 | 6.09  | 39.89 | 9.36 | 0.38 | 0.59 | 49.81 | 16.15 | Malaysia     | [48] |
| Barley straw                            | 84.3  | 10.5  | 5.2   | 41.4  | 6.2  | 0.63 | 0.01 | 51.7  | 15.7  | Canada       | [51] |
| Flax straw                              | 87.2  | 3.3   | 9.6   | 43.1  | 6.2  | 0.68 | 0.09 | 49.9  | 17    | Canada       | [51] |
| Corn straw                              | 82.6  | 8.1   | 12.9  | 42.65 | 5.57 | 1.49 | -    | 49.16 | 16.24 | Ghana        | [16] |
| Barley straw                            | 77.9  | 6.1   | 16    | 40.69 | 6.95 | 1.64 | 0.23 | 50.5  | 17.37 | Spain        | [22] |
| Rye straw                               | 79.9  | 3.2   | 16.9  | 40.18 | 6.85 | 1.16 | 0.32 | 51.48 | 17.11 | Spain        | [22] |
| Wheat straw                             | 76    | 5.3   | 18.19 | 45.58 | 6.04 | 1.18 | 0.59 | 46.6  | 17.34 | Spain        | [22] |
| Wheat straw                             | 68.23 | 17.04 | 14.72 | 45.69 | 6.84 | 1.4  | 0.25 | 45.81 | 14.86 | Mexico       | [52] |
| Wheat straw                             | 73.9  | 4.6   | 21.1  | 46.2  | 6.3  | 0.41 | 0.01 | 47.11 | 15.6  | Canada       | [53] |
| Wheat straw                             | 74.8  | 8.64  | 16.5  | 40.6  | 6    | 0.19 | 0.9  | 53.2  | 17.62 | India        | [38] |
| Herbaceous and Agricultural Grass (HAG) |       |       |       |       |      |      |      |       |       |              |      |
| Timothy grass                           | 82    | 1.2   | 16.8  | 42.4  | 6    | 1.03 | 0.15 | 50.4  | 16.7  | Canada       | [51] |
| Miscanthus                              | 79    | 9.6   | 11.4  | 47.09 | 6.3  | 0.1  | 0.1  | 46.42 | 18.07 | Spain        | [22] |
| Timothy grass                           | 76.1  | 4.4   | 19.5  | 49.3  | 7.1  | 1.5  | 0.1  | 42    | 18.6  | Canada       | [54] |
| Switch grass                            | 82.58 | 2.86  | 14.56 | 50.25 | 6.51 | 0.36 | 0.08 | 42.8  | 18.87 | USA          | [27] |
| Timothy grass                           | 82.8  | 3.1   | 13.3  | 45.1  | 6.3  | 1.3  | 0.1  | 47.1  | 15.9  | Canada       | [53] |
| Napier grass                            | 81.51 | 1.75  | 16.74 | 49.48 | 6.12 | 1.01 | 0.33 | 43.07 | 18.11 | Malaysia     | [55] |
| Grass                                   | 76.5  | 13    | 10.81 | 42    | 5.21 | 2.03 | -    | 50.95 | 16.77 | Brazil       | [44] |
| Green banagrass                         | 76.6  | 6.9   | 16.5  | 48.2  | 5.56 | 0.36 | 0.07 | 45.81 | 17.8  | USA          | [56] |
| Purple banagrass                        | 74.5  | 7.9   | 17.6  | 47.5  | 5.53 | 0.43 | 0.06 | 46.48 | 17.6  | USA          | [56] |
| Guinea grass                            | 73.5  | 8.2   | 18.4  | 47.3  | 5.42 | 0.33 | 0.06 | 46.89 | 17.4  | USA          | [56] |
| <i>Imperata cylindrica</i>              | 77.27 | 3.19  | 19.54 | 44.38 | 5.65 | 0.82 | 0.09 | 49.06 | 18.39 | Brunei       | [57] |
| <i>Imperata cylindrica</i>              | 82.79 | 0.9   | 16.31 | 43.19 | 5.92 | 0.59 | 0.14 | 50.17 | 17.03 | Nigeria      | [58] |
| Elephant grass                          | 72.54 | 8.26  | 19.2  | 39.63 | 6.31 | 1.7  | 0.2  | 52.16 | 15.77 | Brazil       | [59] |
| Wood and Woody Biomass (WWB)            |       |       |       |       |      |      |      |       |       |              |      |
| Pinewood                                | 87.5  | 1.6   | 10.3  | 49    | 6.4  | 0.14 | 0.01 | 44.4  | 19.6  | Canada       | [51] |
| <i>Cytisus multiflorus</i> (Shoot)      | 82.48 | 1.32  | 16.2  | 46.8  | 6.97 | 1.26 | -    | 44.93 | 22.25 | Portugal     | [60] |
| <i>Erica australis</i> (shoot)          | 80.72 | 1.38  | 17.9  | 50.54 | 7.14 | 0.64 | -    | 41.64 | 24.12 | Portugal     | [60] |
| <i>Pterospartum tridentatum</i> (shoot) | 81.1  | 1.44  | 17.45 | 48.64 | 7.07 | 0.68 | -    | 43.57 | 21.37 | Portugal     | [60] |
| <i>Ulex europaeus</i> (shoot)           | 84.46 | 1.47  | 14.06 | 47.01 | 6.95 | 0.96 | -    | 45.03 | 21.87 | Portugal     | [60] |
| <i>Cytisus multiflorus</i> (Shoot)      | 80.81 | 1.37  | 17.83 | 48.51 | 6.51 | 2.04 | -    | 42.91 | 22.26 | Spain        | [60] |
| <i>Erica australis</i> (shoot)          | 79.65 | 1.38  | 18.97 | 49.23 | 6.22 | 0.84 | -    | 43.67 | 24.4  | Spain        | [60] |

|  |       |      |       |       |      |      |      |       |       |               |      |
|--|-------|------|-------|-------|------|------|------|-------|-------|---------------|------|
| <i>Pterospartum tridentatum</i> (shoot)        | 80.32 | 1.21 | 18.47 | 49.41 | 6.74 | 0.97 | -    | 42.84 | 22.14 | Spain         |      |
| <i>Ulex europaeus</i> (shoot)                  | 80.8  | 1.56 | 17.64 | 49.11 | 6.52 | 1.73 | -    | 42.6  | 21.24 | Spain         |      |
| Mango stem                                     | 83.5  | 4.5  | 12    | 50.28 | 6.08 | 0.14 | 0.01 | 43.47 | 16.9  | Tanzania      | [15] |
| Softwood                                       | 85.3  | 0.41 | 14.27 | 47.7  | 5.7  | 0.96 | 0.16 | 45.5  | 18    | South Africa  | [21] |
| Hardwood                                       | 84.7  | 0.48 | 14.82 | 46.4  | 5.5  | 0.1  | 0.01 | 48    | 18    | South Africa  |      |
| Pine chips                                     | 81.6  | 0.6  | 17.8  | 48.15 | 5.59 | 0.09 | 0.28 | 45.9  | 19.43 | Spain         |      |
| Pine shaving                                   | 85    | 0.8  | 14.2  | 48.67 | 5.08 | 0.07 | 0.26 | 45.92 | 19.79 | Spain         | [22] |
| Chestnut tree shaving                          | 79    | 0.4  | 20.6  | 45.88 | 5    | 0.12 | 0.27 | 48.73 | 17.62 | Spain         |      |
| Pine sawdust                                   | 84.58 | 2.24 | 13.18 | 50.3  | 6    | 0.69 | -    | 42.99 | 18.44 | India         | [61] |
| Sal sawdust                                    | 83.31 | 1.25 | 15.44 | 49.83 | 6.01 | 0.58 | -    | 43.56 | 18.2  | India         |      |
| Coffee (Primary branch)                        | 80.62 | 2.42 | 16.95 | 50.31 | 6.13 | 0.92 | 0.36 | 42.28 | 19.2  | Brazil        | [25] |
| Coffee stem                                    | 83.7  | 1.67 | 14.62 | 50.64 | 6.12 | 1.86 | 0.21 | 41.16 | 19    | Brazil        | [53] |
| Pine wood                                      | 76.9  | 2.5  | 20.6  | 50    | 6.3  | 0.1  | 0.1  | 43.5  | 18.1  | Canada        |      |
| <i>Ceiba pentandra</i>                         | 82.43 | 4.72 | 12.85 | 55.26 | 5.3  | 0.48 | 0.05 | 38.91 | 20.33 | Ghana         |      |
| <i>Triplochiton scleroxylon</i>                | 80.97 | 2.01 | 17.02 | 56.83 | 4.08 | 0.56 | 0.09 | 38.44 | 21.6  | Ghana         |      |
| <i>Aningeria robusta</i>                       | 75.23 | 5.04 | 19.73 | 55.08 | 3.83 | 0.48 | 0.21 | 40.4  | 20.89 | Ghana         | [62] |
| <i>Terminalia superba</i>                      | 79.64 | 2.96 | 17.4  | 56.29 | 3.88 | 0.62 | 0.06 | 39.15 | 22.22 | Ghana         |      |
| <i>Piptadenia africana</i>                     | 80.6  | 0.61 | 18.79 | 57.65 | 4.2  | 0.71 | 0.05 | 37.39 | 22.17 | Ghana         |      |
| <i>Celtis mildbreadii</i>                      | 83.7  | 3.71 | 12.59 | 55.85 | 4.21 | 0.69 | 0.06 | 39.19 | 20.16 | Ghana         |      |
| Grape stem                                     | 73    | 6    | 22    | 52.04 | 6.37 | 1.06 | 0.16 | 40.36 | 19    | Spain         | [28] |
| Pine   | 84.46 | 0.36 | 15.18 | 50.8  | 6.06 | 0.3  | 0.01 | 42.82 | 19.91 | Spain         |      |
| Black Poplar                                   | 82.31 | 1.1  | 16.59 | 50.4  | 5.96 | 0.39 | 0.02 | 43.23 | 19.63 | Spain         | [63] |
| Chestnut                                       | 82.28 | 0.31 | 17.41 | 49.81 | 5.66 | 0.26 | 0.01 | 44.26 | 19.08 | Spain         |      |
| Almond tree                                    | 75.03 | 4.56 | 20.41 | 50.91 | 5.84 | 0.94 | 0.23 | 42.08 | 19.39 | USA           | [39] |
| Pine wood                                      | 81.4  | 2.6  | 16    | 43.28 | 5.1  | 0.35 | -    | 51.27 | 17.94 | South Africa  | [40] |
| Hybrid poplar                                  | 89.4  | 0.8  | 9.8   | 46.7  | 6.1  | 0.4  | -    | 46.8  | 19.6  | USA           | [42] |
| Pine chips                                     | 85.98 | 0.27 | 13.76 | 47.21 | 6.64 | 0.17 | -    | 45.76 | 18.46 | USA           | [64] |
| Logging residue (Pine)                         | 82.17 | 1.77 | 16.07 | 47.29 | 6.2  | 0.42 | -    | 45.19 | 18.79 | USA           |      |
| Yemane tree sawdust                            | 74.47 | 6.68 | 18.85 | 45.42 | 5.91 | 0.51 | -    | 48.16 | 16.29 | India         | [65] |
| Sawdust  | 83.88 | 0.11 | 16    | 50.3  | 6.08 | 0.15 | -    | 43.43 | 20    | Brazil        | [44] |
| <i>E. grandis</i>                              | 88.4  | 0.1  | 11.5  | 48.45 | 7.52 | 0.11 | 0.06 | 43.86 | 19.2  | Uganda        |      |
| <i>T. glaucescens</i>                          | 83.9  | 1    | 15.1  | 48.24 | 7.91 | 0.24 | 0.05 | 43.56 | 19.3  | Uganda        | [66] |
| <i>A. hockii</i>                               | 83.8  | 1.1  | 15.1  | 48    | 7.2  | 0.23 | 0.05 | 44.52 | 19.2  | Uganda        |      |
| <i>C. molle</i>                                | 82.6  | 2.1  | 15.3  | 47.9  | 7.69 | 0.27 | 0.05 | 44.09 | 19.1  | Uganda        |      |
| <i>Gmelina</i>                                 | 80.9  | 1    | 18.1  | 51.9  | 6.3  | 0.16 | -    | 41.64 | 20.8  | Nigeria       |      |
| <i>Terminalia</i>                              | 80.2  | 2.2  | 17.4  | 50.1  | 5.9  | 0.33 | -    | 43.67 | 19.4  | Nigeria       | [46] |
| <i>Lophira</i>                                 | 78.1  | 1.6  | 20.3  | 52.7  | 6.6  | 0.28 | -    | 40.42 | 21.1  | Nigeria       |      |
| <i>Nauclea</i>                                 | 80.6  | 0.7  | 18.8  | 53.5  | 6.3  | 0.64 | -    | 39.56 | 22.9  | Nigeria       |      |
| Wood   | 77.92 | 0.27 | 21.81 | 49.06 | 6.31 | 2.08 | 0    | 42.55 | 18.78 | UK            | [67] |
| <i>A. pedicellaris</i>                         | 92.7  | 1.68 | 5.61  | 51.7  | 5.85 | 0.54 | -    | 42    | 20.1  | Nigeria       |      |
| <i>T. grandis</i>                              | 95.5  | 0.7  | 3.8   | 49.6  | 6.3  | 0.4  | -    | 43.7  | 19.8  | Nigeria       | [49] |
| <i>T. ivorensis</i>                            | 82.3  | 0.32 | 17.4  | 48.6  | 6    | 0.44 | -    | 45    | 17.3  | Nigeria       |      |
| Wood bark<br>( <i>Calophyllum inophyllum</i> ) | 76.9  | 2.43 | 20.66 | 45.68 | 7.65 | 2.14 | 0.66 | 43.87 | 21.14 | India         | [68] |
| Coffee stem bark                               | 75.63 | 4.33 | 20.03 | 54.41 | 6.59 | 2.13 | 0.21 | 36.66 | 19.2  | Brazil        | [25] |
| Palm shells                                    | 75.4  | 4.6  | 20    | 54.02 | 5.98 | 0.38 | 0.03 | 39.54 | 19.29 | Tanzania      | [15] |
| Cocoa beans husk                               | 69    | 9.96 | 21.04 | 43.25 | 5.89 | 2.64 | 0.29 | 47.93 | 17.31 | Spain         | [22] |
| <i>Sorghum bicolor</i> stalk                   | 82.9  | 3.25 | 13.8  | 46.2  | 5.85 | 0.44 | -    | 47.6  | 17.9  | Nigeria       | [49] |
| Wheat straw                                    | 83.3  | 1.4  | 15.3  | 41.6  | 6.1  | 0.14 | 0.06 | 52.1  | 20.3  | Canada        | [51] |
| Wheat straw                                    | 76.3  | 5.2  | 18.5  | 48.53 | 6.25 | 1.5  | 0.16 | 43.57 | 19.96 | Australia     | [37] |
| Switch grass                                   | 84.2  | 3.9  | 11.9  | 43.8  | 6.4  | 0.4  | 0.1  | 49.4  | 19.8  | United States | [69] |
| Coffee (Secondary branch)                      | 75.31 | 3.45 | 21.23 | 51.82 | 6.4  | 1.51 | 0.21 | 40.06 | 19.2  | Brazil        | [25] |

<sup>a</sup> calculated by difference

B. Statistical Analysis and Multivariable Regression Modelling

Regression analysis helps to build a probabilistic model that shows the correlation between a response variable and a single predictor (simple regression) or more than one predictor variables (multiple regression). The MVRA is a robust technique that takes into account the mutual effects of the explanatory variables on the output variable. The model that relates  $n$  independent variables,  $X_i$ , ( $1 \leq i \leq n$ ), and  $m$  dependent variables  $Y_j$ , ( $1 \leq j \leq m$ ) is expressed as (1),

$$Y_j = \sum_{i=1}^n \alpha_n X_n + \beta_j \quad (1)$$

where  $\alpha_i$ , ( $1 \leq i \leq n$ ) is a regression coefficient that depicts the dependence of  $Y_j$  when  $X_i$  changes by one unit, while  $\beta_j$  is a constant termed correction factor and  $j$  is the number of observation. Table 2 presents twelve established and relatively recent HHV models in published literature. For instance, equations. (2) – (11) were formulated in the 1920s for biomass, while equation (12), though for biomass, and equation (13), for coal, are several decades old. These correlation models were selected for the purpose of comparison of the predictive capabilities of the proposed HHV models in this study. To develop a functional relation in terms of the characteristic properties of biomass, the influence of the predictor variables (VM, ash, C, H, N, and S) on the estimation of HHV was initially investigated with the MATLAB *corrcoef* command. This yielded the matrix of Pearson's R, and the  $p$ -values with a non-correlation hypothesis test at a significance level of 5%. Thereafter, a regression analysis was conducted by plugging the data into a spreadsheet and observing the lines of best fits based on ANOVA results. It is noteworthy that primary consideration was given to the statistically significant variables. However, there was an exemption of FC and O variables in the statistical analysis as well as the regression modelling because their measurements were not independently taken. Two statistical parameters (Eqs. 14 and 15), which included, the average absolute error (AAE), and average bias error (ABE) were deployed to study the model performance.

$$AAE = \frac{1}{m} \sum_{j=1}^m \left| \frac{HHV_{pre,j} - \overline{HHV}_{exp}}{HHV_{exp,j}} \right| \times 100\% \quad \text{Eq.14}$$

$$ABE = \frac{1}{m} \sum_{j=1}^m \left( \frac{HHV_{pre,j} - \overline{HHV}_{exp}}{HHV_{exp,j}} \right) \times 100\% \quad \text{Eq.15}$$

Where the  $HHV_{pre}$  and  $HHV_{exp}$  are predicted and the experimental HHV respectively, the bar indicates an average value,  $j$  is the  $j^{th}$  number of  $m$  experimental data. The AAE indicates the discrepancy between the predicted and the experimental values. By implication, a lower AAE signifies a higher accuracy for a given model. On the other hand, a positive ABE value implies an overestimation, while a negative value indicates an underestimation.

Table 2 Selected HHV models for biomass samples from published literature.

| Model No | HHV Equations  | Based on | Unit    | REF  |
|----------|--|----------|---------|------|
| Eq.2     | $HHV = 10.982 + 0.1136 \cdot VM - 0.2848 \cdot ash$  |          | M J/k   | [9]  |
| Eq.3     | $HHV = -17.507 + 0.3985 \cdot VM + 0.2875 \cdot FC$  | P        | g M J/k | [9]  |
| Eq.4     | $HHV = 1.83 \times 10^4 - 3.98 \cdot ash^2 - 112.10 \cdot ash$   | P        | g kJ/kg | [7]  |
| Eq.5     | $HHV = 0.3536 \cdot FC + 0.1559 \cdot VM - 0.0078 \cdot ash$   | P        | M J/k   | [70] |
| Eq.6     | $HHV = 0.1905 \cdot VM + 0.2521 \cdot FC$  | P        | g M J/k | [10] |
| Eq.7     | $HHV = 0.2949 \cdot C + 0.8250 \cdot H$  | P        | g M J/k | [10] |
| Eq.8     | $HHV = 338.4 \cdot C + 244.2$  | U        | g kJ/kg | [8]  |
| Eq.9     | $HHV = 1.87 \cdot C^2 - 144 \cdot C - 2820 \cdot H + 68.3 \cdot C \cdot H + 129 \cdot N + 20147$             | U        | kJ/kg   | [71] |
| Eq.10    | $HHV = 5.22 \cdot C^2 - 319 \cdot C - 1647 \cdot H + 38.6 \cdot C \cdot H + 133 \cdot N + 21028$             | U        | kJ/kg   | [71] |
| Eq.11    | $HHV = 0.3491 \cdot C + 1.1783 \cdot H - 0.1005 \cdot S - 0.1034 \cdot O - 0.015 \cdot N - 0.0211 \cdot ash$ | U        | M J/k g | [72] |
| Eq.12    | $HHV = 0.4373 \cdot C - 1.6701$  | U        | M J/k g | [73] |
| Eq.13    | $HHV = 0.336 \cdot C + 1.418 \cdot H - (0.153 \cdot O + 0.0941 \cdot S)$                                     | U        | M J/k g | [5]  |

P – proximate; U – ultimate

III. RESULTS AND DISCUSSION

A. Statistical Analysis and Multivariable Regression Modelling

The R and p statistics represent the correlation coefficients, and the probability of obtaining a correlation by chance respectively. Table 3 presents the aforementioned statistic parameters for the selected variables in relation to HHV estimation.

**Table 3** R and p values for HHV related to proximate and ultimate analyses

|      | VM   | Ash  | C    | H    | N     | S    |
|------|------|------|------|------|-------|------|
| R    | 0.32 | -    | 0.51 | 0.11 | 0.088 | -    |
| valu | 06   | 0.55 | 62   | 35   | 26    | 0.06 |
| es   |      | 20   |      |      |       | 46   |
| P    | 0.00 | 0.00 | 0.00 | 0.14 | 0.252 | 0.40 |
| valu | 00   | 00   | 00   | 05   | 4     | 27   |
| es   |      |      |      |      |       |      |

The statistically significant correlation is demonstrated by VM, Ash and C contents as indicated by the p-values < 0.05. The strongest relationship exists for the ash content, albeit, with a negative effect, while in sequence, a positive correlation exist for C and H. However, the influence of the other variables is statistically negligible.

**Table 4** Developed HHV models and their regression statistics

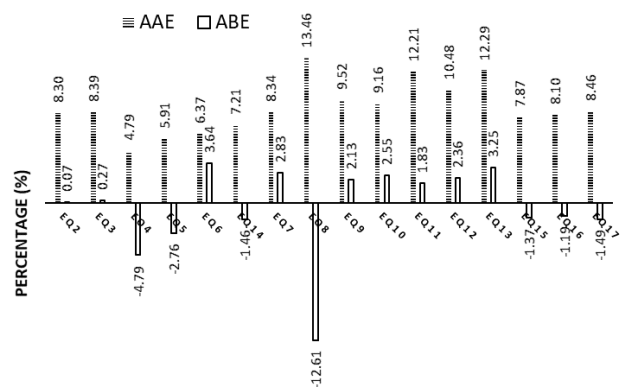
| Model No | Equation                   | R <sup>2</sup> | Adjusted R <sup>2</sup> | Standard Error | Significance F             |
|----------|----------------------------|----------------|-------------------------|----------------|----------------------------|
| Eq.14    | 0.2351 · VM – 0.0775 · ash | 0.985          | 0.977                   | 2.257          | 4.306 × 10 <sup>-122</sup> |
| Eq.15    | 0.3399 · C + 0.3590 · H    | 0.986          | 0.979                   | 2.149          | 6.098 × 10 <sup>-125</sup> |
| Eq.16    | 0.3787 · C + 2.3245 · S    | 0.987          | 0.979                   | 2.130          | 2.310 × 10 <sup>-125</sup> |
| Eq.17    | 0.3769 · C + 0.462 · N     | 0.986          | 0.979                   | 2.154          | 8.802 × 10 <sup>-125</sup> |

<sup>b</sup> both variables

Table 4 presents the empirical models developed through the MVRA technique based on proximate and ultimate analysis data in this study. Following the non-correlation hypothesis test, variables were considered in succession utilizing a stepwise regression technique. It is shown that the estimations of the lines of “best-fit” for the models are high with the least, R<sup>2</sup> = 0.985, being the model proposed from proximate analysis data. It is important to note that C variable features prominently in the functional relations. This attests to the fact that it contributes significantly to the energy content of biomass resources [10], [74]. The proposed models, equations 14-17, are relatively simple linear relations

free of some common mathematical blunders noted earlier, that is, the inclusion of FC and O variables [1], [7], [71].

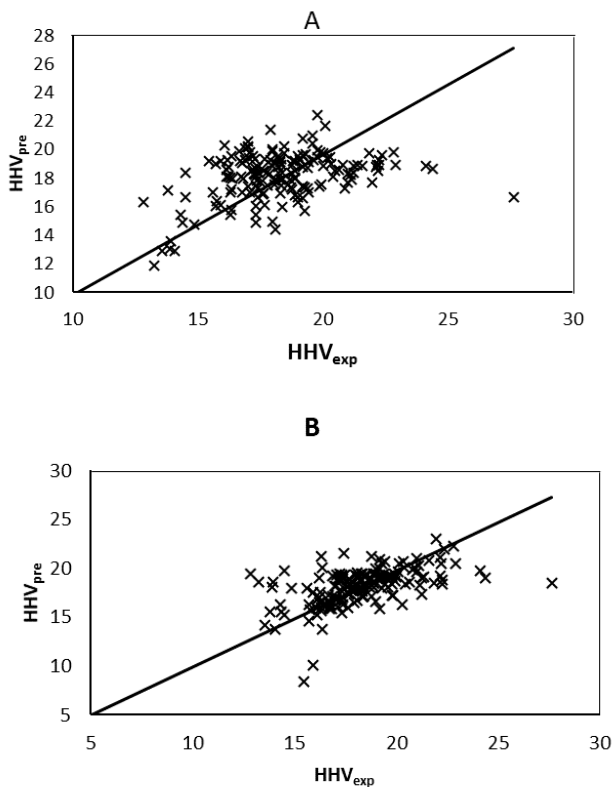
Sequel to the incorporation of the validation data, HHVs were approximated using equation 2-17 and model performance was undertaken. Figure 1 shows the values of AAE and ABE parameters for the empirical relations developed in this study and those from other published literature. Unlike some previous correlations (equations 8, 12, 13), all the developed models have the capability to estimate biomass HHV's with an AAE less than 10%, suggesting a relatively higher accuracy. In addition, it may be inferred that the accuracy of a model is not necessarily dependent on the inclusion of large number of predictor variables as aptly illustrated by equations 11 and 13. Contrary to the report by Yin et al [10], the values of AAE for some of the correlations derived from proximate data compares favorably well with those of ultimate data. In fact, equations 14 and 15 respectively are 7.21 and 7.87%. It is noteworthy that both models have absolute values of ABE less than 2.0%. In real terms, however, they are both negative values implying a tendency for low underestimation. This is significant because of its practical utility in less developed countries of Africa, where accessibility to sophisticated analytical instruments and the requisite expertise could be a challenge. Therefore, equation 14 particularly, provides a handy and a simple tool for HHV estimation from the results of much less complicated experiments such as proximate analysis. The empirical models developed from ultimate analysis data have the least absolute values of ABE (1.19 to 1.49) relative to previously published models (1.83 to 12.61); implying a minimal bias error in their predictive capabilities. Additionally, equation 15 presents the lowest AAE with a 0.06% underestimation of 1.37% among the models in the ultimate analysis. This attests to its high predicative capability.



**Figure 1** Plot of AAE and ABE of the 16 HHV models.

Figures 2a and 2b respectively compare the predicted and measured HHV based on Eqs. 14 and 15 for all biomass materials under investigation. It is demonstrated that Figure 2b has far less number of outliers that is an indication that Eq. 15 provides a

relatively more accurate correlation. This is in agreement with a previous report [10].



**Figure 2** Plot of predicted and experimental HHV for the proposed model based on (A) proximate analysis – equation 14 and (B) ultimate analysis – equation 15

#### CONCLUSION

This research sought to develop an HHV prediction model for biomass of diverse origin through the use of a MVAR technique. The correlations obtained from this study demonstrated relatively higher level of accuracy and lower tendency for overestimation. The prediction model from proximate analysis is highly recommended because of its simplicity and suitability within the African context in the determination of energy values of biomass materials.

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