

# Investigation of Motorcycle Design Improvements with Respect to Whole Body Vibration Exposure to the Rider

Ndimila .W. Benjamin; Majaja. A. Bashira; Elias Erasto and Nalitolela .G. Noel

Department of Mechanical and Industrial Engineering,  
College of Engineering and Technology,  
University of Dar es Salaam.  
Dar es Salaam, Tanzania

Email: benjaminndimila@yahoo.com; bamajaja@yahoo.com; ebelias@udsm.ac.tz; nnalitolela@gmail.com.

**Abstract**—Various studies on motorcycle rider whole body vibration (WBV) exposure indicate that the vibration magnitude in the vertical direction is the most severe as compared to magnitudes in lateral and transverse directions. For the sake of understanding and doing evaluation of the vibration environment of the motorcycle rider and various motorcycle component bodies, a mathematical model was developed. The main intention was to investigate the physics of motorcycle suspensions, study vibration magnitudes in vertical direction in terms of displacement and acceleration on a cyclist depending on motorcycle and road parameters, also attempt to determine the location of the rider's seat with least vibration magnitudes. In this case, analytical methods for studying response to harmonic base excitation of the rider and other component bodies of a motorcycle were applied with the aim to analyze their vibrational behaviour. The two wheeled motorcycle with a rider model was introduced. The equations of motion for the model were formulated. The matrix form of the equations was written solved and simulations were done. The vibration behaviour in vertical direction of various component bodies of the motorcycle model was observed.

**Keywords**—*modeling, Motorcycle rider, vibration magnitude*

## I. INTRODUCTION

In recent days modeling has become a major process in the quest for determining, improving, and optimizing dynamic characteristics of engineering systems. Model creation and analysis of a particular vibration system involves the process of determining the inherent dynamic characteristics of the system in terms of spring characteristics and damping factors which facilitates the formulation of mathematical model for analysis of the dynamic behaviour. Modeling is regarded as part of solution of an engineering problem that aims at producing its mathematical description. This description can be obtained by taking advantage of known laws of physics. The laws cannot be directly applied to real systems; therefore it becomes necessary to introduce many assumptions that simplify the engineering

problem to such an extent that physics laws may be applied [6]. Modeling a mechanical system begins with creation of a physical model on which physics laws and mathematical operations are applied to develop a mathematical model [11]. The process of solving the mathematical model is known as analysis and yields the solution to a problem considered.

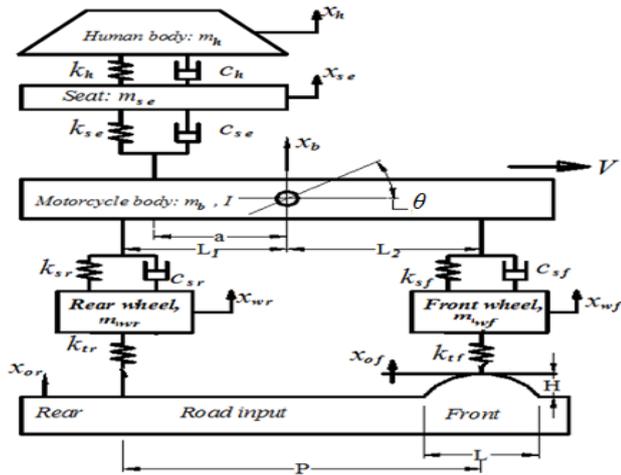
When riding a motorcycle the type of disturbance mostly affecting comfort of the rider, is random vibration which is caused by unpredicted loads such as road roughness and wind. Human exposure to whole-body vibration results into transmission of vibratory energy to the entire body and leads to localized effects. It affects comfort, normal functioning of the body and health [8], [9]. Recently, [3] carried out a WBV exposure comparison between motorcycles and cars. They concluded that WBV exposure levels of common motorcycle riders are distinctively higher than those of car drivers. Reference [12] also found that motorcycle riders have higher health risks than car drivers because they are sitting on a flat seat without back support causing greater energy absorption of vertical vibrations. A study done to investigate vibration magnitudes to which commercial motorcycle riders of the Dar es Salaam city were subjected, found that magnitudes in Z axis (vertical direction) were the highest as compared to magnitudes in X and Y axes [2]. These results lead to a desire of using mathematical descriptions to investigate the motorcycle construction with respect to vibration magnitudes of various parts including the rider, caused by the nature of terrain.

## II. MATHEMATICAL MODEL FORMULATION

A motorcycle with rider model is considered, taking into account pitch motion of the motorcycles' body. The degrees of freedom considered are; motorcycle vertical body displacement  $x_b$ , motorcycle body pitch angle  $\theta$ , front wheel displacement  $x_{wf}$  and rear wheel displacement  $x_{wr}$ . The rider body is represented as  $m_h$ , the front wheel of the motorcycle is represented by the mass  $m_{wf}$ , and the spring coefficient  $K_{tf}$ . Similarly the rear wheel is represented by the mass  $m_{wr}$ , and the spring coefficient  $K_{tr}$ . The suspensions of the front and rear wheels are described by the damper's coefficients  $C_{sf}$  and  $C_{sr}$  and the spring's coefficients  $K_{sf}$  and  $K_{sr}$  respectively. The mass  $m_b$  and the inertia  $I$

represent the motorcycle body sprung mass. The location of the center of gravity is given by  $L_1$  and  $L_2$ . Typical parameters for lumped seated human coupled with a motorcycle model listed in Table .1, were determined using different methods (experimental methods and reviewing various literature) which ensured that the parameters were actual for various motorcycle components and human. The schematic diagram of lumped seated human coupled with a Motorcycle vibration model is shown in Fig. 1

The human-body has been considered as a lumped mass with stiffness ( $k_h$ ) and damping ( $C_h$ ) properties obtained from those proposed by [1].



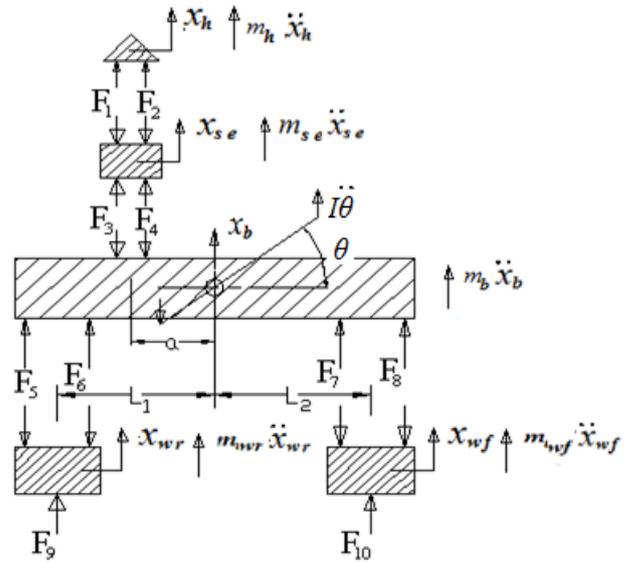
**Figure1:** Schematic diagram of lumped seated human coupled with a Motorcycle vibration model.

**Table 1.** Parameters for lumped seated human coupled with a Motorcycle vibration model.

Model parameter	Symbol	Value	
Front / rear tire stiffness (N/m).	$K_{yf} / K_{tr}$	130,000/ 141,000	Sharp <i>et al.</i> , (2004)
Front /rear wheel and axle masses (Kg).	$m_{wf} / m_{wr}$	11.9/ 14.7	measured
Linear front and rear suspension damping Coefficients (N·s/m).	$C_{sf} / C_{sr}$	2134/ 1165	measured
Front and rear suspension stiffness (N/m).	$K_{sf} / K_{sr}$	25000/ 58570	measured
Distance between the C.G and front axle (m).	$L_1$	0.70	calculated
Distance between the C.G and rear axle (m).	$L_2$	0.595	calculated
Distance between the C.G and seat (m).	$a$	0.298	calculated
Motorcycle body mass (sprung mass) (Kg).	$m_b$	119	measured
Rider body mass (kg)	$m_h$	60.67	Abbas <i>et al.</i> ,2013
Rider body stiffness properties	$k_h$	390330	
Rider body damping properties	$C_h$	4224.1	
Motorcycle body mass moment of inertia (Kg·m <sup>2</sup> ).	$I$	22.013	calculated
Seat mass (Kg).	$m_{se}$	14.8	measured
Seat damping Coefficients (N·s/m).	$C_{se}$	150	measured
Seat suspension stiffness (N/m).	$K_{se}$	15,000	measured

### A. Derivation of Equations of Motion

Schematic diagram of lumped seated human coupled with a Motorcycle vibration model was further simplified into free body diagrams of constituent bodies (Fig. 2).



**Figure 2** Free Body Diagrams of component bodies of the Model

Assuming conditions of dynamic equilibrium to the component bodies constituting the model in Fig. 2, the equations 1 to 10 for various vertical forces acting on constituent bodies of the model were formulated.

$$F_1 = k_h(x_{se} + x_h) \quad (1)$$

$$F_2 = c_h(\dot{x}_{se} - \dot{x}_h) \quad (2)$$

$$F_3 = k_{se}(x_b - x_{se} - a\theta) \quad (3)$$

$$F_4 = c_{se}(\dot{x}_b - \dot{x}_{se} - a\dot{\theta}) \quad (4)$$

$$F_5 = k_{sr}(x_{wr} - x_b + L_1\theta) \quad (5)$$

$$F_6 = c_{sr}(\dot{x}_{wr} - \dot{x}_b + L_1\dot{\theta}) \quad (6)$$

$$F_7 = k_{sf}(x_{wf} - x_b - L_2\theta). \quad (7)$$

$$F_8 = c_{sf}(\dot{x}_{wf} - \dot{x}_b - L_2\dot{\theta}) \quad (8)$$

$$F_9 = k_{tr}(x_{or} - x_{wr}) \quad (9)$$

$$F_{10} = k_{tf}(x_{of} - x_{wf}) \quad (10)$$

Applying Newton's equations of motion for each body, equations 11-16 were formulated:

$$m_h\ddot{x}_h - F_1 - F_2 = 0 \quad (11)$$

$$m_{se}\ddot{x}_{se} + F_1 + F_2 - F_3 - F_4 = 0 \quad (12)$$

$$m_b\ddot{x}_b + F_3 + F_4 - F_5 - F_6 - F_7 - F_8 = 0 \quad (13)$$

$$I\ddot{\theta} - L_2F_7 - L_2F_8 - aF_3 - aF_4 + L_1F_5 + L_1F_6 = 0 \quad (14)$$

$$m_{wf}\ddot{x}_{wr} - F_{10} + F_7 + F_8 = 0 \quad (15)$$

$$m_{wr}\ddot{x}_{wr} - F_9 + F_5 + F_6 = 0 \quad (16)$$

For such a multi degrees of freedom system, the six equations of motions for the five bodies can be combined, rearranged and expressed in matrix form as equation 17.

$$[M]\{\ddot{x}\} + [C]\{\dot{x}\} + [K]\{x\} = \{F(t)\} \quad (17)$$

Where the force, displacement, velocity and acceleration vectors and also the mass, damping and stiffness matrices would be written as follows:

$$\{F(t)\} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ k_{tf}x_{of} \\ k_{tr}x_{or} \end{bmatrix}, \{x\} = \begin{bmatrix} x_h \\ x_{se} \\ x_b \\ \theta \\ x_{wf} \\ x_{wr} \end{bmatrix}, \{\dot{x}\} = \begin{bmatrix} \dot{x}_h \\ \dot{x}_{se} \\ \dot{x}_b \\ \dot{\theta} \\ \dot{x}_{wf} \\ \dot{x}_{wr} \end{bmatrix}, \{\ddot{x}\} = \begin{bmatrix} \ddot{x}_h \\ \ddot{x}_{se} \\ \ddot{x}_b \\ \ddot{\theta} \\ \ddot{x}_{wf} \\ \ddot{x}_{wr} \end{bmatrix}$$

$$[M] = \begin{bmatrix} m_h & 0 & 0 & 0 & 0 & 0 \\ 0 & m_{se} & 0 & 0 & 0 & 0 \\ 0 & 0 & m_b & 0 & 0 & 0 \\ 0 & 0 & 0 & I & 0 & 0 \\ 0 & 0 & 0 & 0 & m_{wf} & 0 \\ 0 & 0 & 0 & 0 & 0 & m_{wr} \end{bmatrix}$$

$$[C] = \begin{bmatrix} c_h & -c_h & 0 & 0 & 0 & 0 \\ -c_h & c_h + c_{se} & -c_{se} & ac_{se} & 0 & 0 \\ 0 & -c_{se} & c_{sf} + c_{sr} + c_{se} & c_{sf}L_2 - c_{sr}L_1 - ac_{se} & -c_{sf} & -c_{sr} \\ 0 & ac_{se} & L_2c_{sf} - L_1c_{sr} - ac_{se} & L_1^2c_{sr} + L_2^2c_{sf} + a^2c_{se} & -L_2c_{sf} & L_1c_{sr} \\ 0 & 0 & -c_{sf} & -c_{sf}L_2 & c_{sf} & 0 \\ 0 & 0 & -c_{sr} & c_{sr}L_1 & 0 & c_{sr} \end{bmatrix}$$

$$[K] = \begin{bmatrix} k_h & -k_h & 0 & 0 & 0 & 0 \\ -k_h & k_{se} + k_h & -k_{se} & ak_{se} & 0 & 0 \\ 0 & -k_{se} & +k_{sr} + k_{se} + k_{sf} & k_{sf}L_2 - k_{sr}L_1 - ak_{se} & -k_{sf} & -k_{sr} \\ 0 & ak_{se} & L_2k_{sf} - L_1k_{sr} - ak_{se} & a^2k_{se} + L_1^2k_{sr} + L_2^2k_{sf} & -L_2k_{sf} & L_1k_{sr} \\ 0 & 0 & -k_{sf} & -k_{sf}L_2 & k_{sf} + k_{sr} & 0 \\ 0 & 0 & -k_{sr} & k_{sr}L_1 & 0 & k_{sr} + k_{sf} \end{bmatrix}$$

### B. Description of Input Profile Excitations

In this work, the sinusoidal road profiles excitation used in [1] is adopted to evaluate the proposed system. The sinusoidal road equations are as follows in equations 18 and 19:

$$x_{of} = H\sin(\omega t) \quad (18)$$

$$x_{or} = H\sin(\omega(t + \tau)) \quad (19)$$

Where,  $\omega$  is the radian frequency of the road and is equal to  $\pi V/L$ .

Mathematical model of road profile is derived assuming motorcycle with wheelbase  $p$  passing over humps with speed  $V$ , will have front ground displacement  $x_{of}$ . The rear ground  $x_{or}$  follows the same track as the front with a given time delay  $\tau$  (wheelbase correlation) which is equal to the wheelbase divided by the motorcycle speed ( $\tau = p / v$ .) This study assumed that the model travels with the constant speed of 20 km/h (5.5 m/s),  $H = 0.035$ m; is the hump height, and ( $L = 1$  m) is the length of the hump. The displacement and acceleration for the model in terms of time domain were obtained by solving derived equations of motion using MATLAB/ SIMULINK software version 7.9.0529(R2009b). The initial conditions were assumed at equilibrium position. In this assumption, the rider was seated, and therefore, the initial velocity and displacement for each mass were equal to zero.

Substituting the given values in equations 18 and 19, the input excitations were written as:

$x_{of} = 0.035\sin(17.27t)$  and  $x_{or} = 0.035\sin(17.27t + 4.066)$ , hence the force vector were written in a form of a single column matrix in Equation 20

$$\{F(t)\} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 4550\sin(17.27t) \\ 4935\sin(17.27t + 4.066) \end{bmatrix} \quad (20)$$

Input excitations caused by the road profile were introduced to the model through two points representing a modal front and rear wheels. The road profile caused the displacements  $x_{wf}$  and  $x_{wr}$  in vertical direction as motorcycle model was simulated travelling along a path with harmonic profile at constant speed. By doing model simulation, it was possible to observe vertical motion responses of all model components at a given instant.

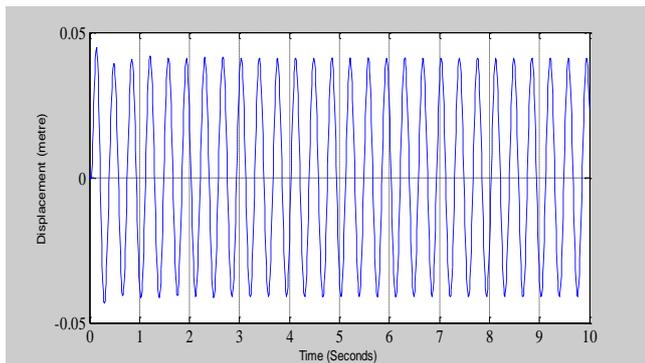
The MATLAB software was used for solving, simulating and plotting the vibrational displacement and acceleration responses of the rider and other component bodies of a motorcycle for the assumed harmonic base excitations.

### III. OBSERVATIONS FROM THE MODEL SIMULATION AND RESULTS

#### A. Model front wheel response

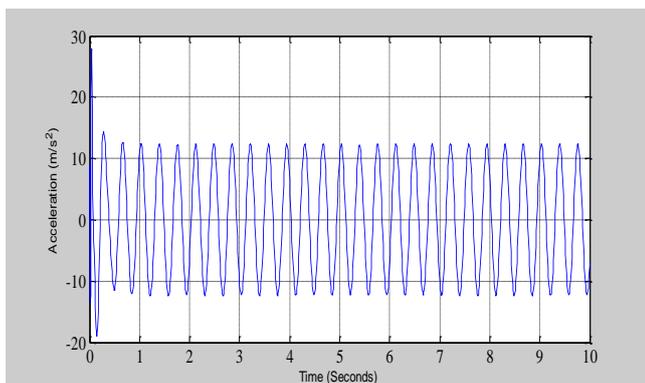
Response of a model front wheel to the road profile excitations resulted into varying vertical displacement ( $x_{wf}$ ) forming a graphical profile similar to sine wave, attaining an amplitude value of 0.041m after stabilization. This could be described as a vibrational state of a wheel caused by the nature of the terrain as the model motorcycle travels at a given speed. The amplitude displacement value (Fig. 3) was slightly above the hump height ( $H = 0.035$ ), This could be described as a result of inertia effects and elastic

properties on the frontal wheel on striking a hump profile at a speed resulting into motorcycle body pitch motion about a small angle  $\theta$ .



**Figure 3** Simulation results: Vibration vertical displacement of the model front wheel ( $x_{wf}$ ) in time domain (amplitude after stabilization= 0.041m)

The front wheel of the model attained a very high acceleration ( $\ddot{x}_{wf}$ ) in the beginning and stabilized at an amplitude of  $12.329\text{m/s}^2$  after a first seconds as seen in Fig. 4



**Figure 4** Simulation results: Vibration vertical acceleration of the model front wheel ( $\ddot{x}_{wf}$ ) in time domain (amplitude after stabilization=  $12.329\text{ m/s}^2$ )

#### B. Model rear wheel response

The response of the model rear wheel did not differ much from those of the front wheel in profile, but there were significant differences in both vibration displacement and acceleration magnitudes. The rear wheel attained displacement amplitude of  $0.035\text{m}$  almost equal to the hump height  $H$  (Fig. 5), and acceleration amplitude of  $10.500\text{m/s}^2$  (Fig. 6) after stabilization. The magnitude of vibration displacement being equal to the value of the profile hump height, to some extent describes the correctness of the model as during the pitch motion while the frontal wheel raising up, the rear wheel tended to travel the opposite side hence tracing the hump profile. The vibration displacement and acceleration magnitudes were slightly less than those attained by the frontal modal wheel. This difference could have been brought about by the difference in weight ( $m_{ff}$  and  $m_{tr}$ ) also stiffness properties ( $k_{ff}$  and  $k_{tr}$ ) between the model wheels. Motorcycles are manufactured with such a difference in characteristics between front and rear

wheel because of the fact that, when it is travelling at speed, there exists a tendency of decrease in the load on the front wheel and a corresponding increase in load on the rear wheel [5]. The dimensions, stiffness and other properties for the rear wheel are greater than those of the front wheel to make it withstand these changes in load.

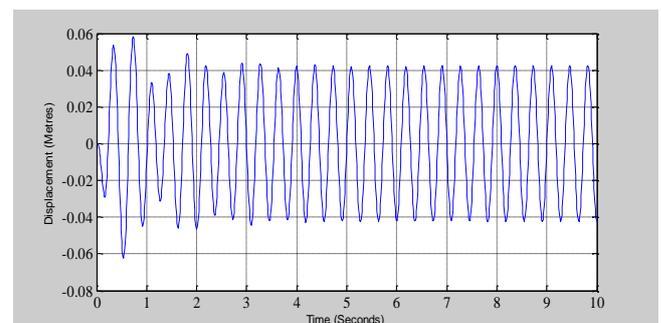
#### C. Model body responses

The motorcycle body was represented by the sprung mass  $m_b$  and mass moment of inertia  $I$ , hence its responses were described by the vertical displacement  $x_b$  and pitch angle  $\Theta$ . In simulation results for motorcycle body displacement and acceleration, the amplitudes attained after stabilization were  $0.024\text{m}$  and  $7.148\text{m/s}^2$  respectively. As the vibration reaching the body originates from the front and rear wheels, comparatively there is a high reduction in vibration magnitudes. This difference may have been caused by two physical reasons namely, big mass value  $m_b$  as compared to  $m_{wf}$  and  $m_{wr}$  also the existence of the suspension system separating the tyres from the body (sprung mass). According to Newton's second law of motion for a given force, the acceleration of a body is inversely proportion to its mass. Some of the vibration energy from the tyres might have been absorbed by the suspension springs and dampers systems and hence resulting in reduced vibration magnitude values.

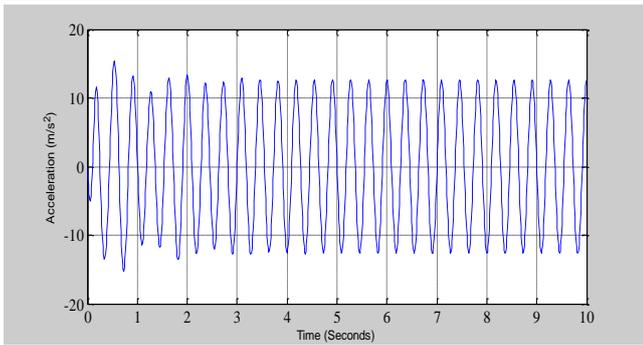
Pitch motion results produced the highest vibration magnitudes as compared to vibration magnitudes of all other constituent bodies of a model. The highest amplitude attained after stabilization were  $0.047\text{m}$  for vibration displacement and  $13.943\text{ m/s}^2$  for vibration acceleration

#### D. Model seat and rider responses

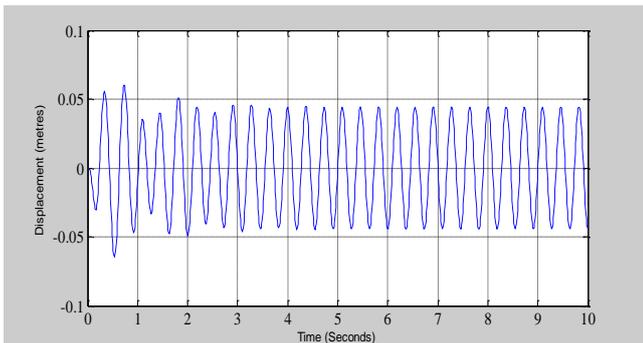
Although they had different magnitudes, the responses of the model seat and rider had similar behaviour. Both the graphs for  $x_{se}$  and  $x_h$  began with 0 followed by a negative inclement accompanied by high fluctuations attaining stable amplitude after the end of the first second. Both displacement and acceleration responses behaved in a similar manner. The vibrational acceleration and displacement of model rider and seat in terms of time domain were as indicated in Figures 5- 8.



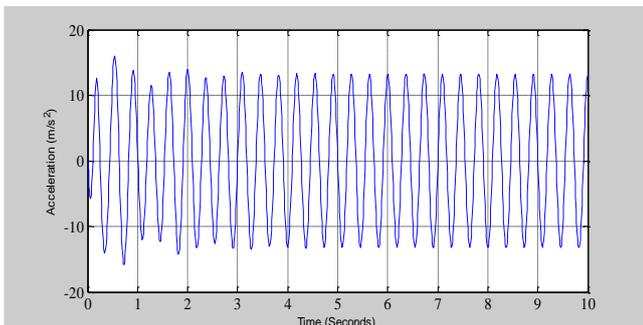
**Figure 5** Simulation results: Vibration vertical displacement of the model seat ( $x_{se}$ ) in time domain (amplitude after stabilization=  $0.042\text{m}$ )



**Figure 6** Simulation results: Vibration vertical acceleration of the model seat  $\ddot{x}_{se}$  in time domain (amplitude after stabilization =  $12.632 \text{ m/s}^2$ )



**Figure 7** Simulation results: Vibration vertical displacement of the model rider ( $x_h$ ) in time domain (amplitude after stabilization =  $0.044 \text{ m}$ )



**Figure 8** Simulation results: Vibration vertical acceleration of the model rider  $\ddot{x}_h$  in time domain (amplitude after stabilization =  $13.223 \text{ m/s}^2$ )

#### IV. INVESTIGATION ON MODEL VIBRATION BEHAVIOUR WITH RESPECT TO PARAMETER CHANGES

The model simulation results were investigated with the aim of having an over view on how vibration magnitudes behaved with changing parameters of the model components. The investigation began by making alterations in the following parameters of the model: the position of the seat relative to the position of the center of gravity (parameter  $a$ ) and rear suspension system stiffness (parameter  $k_{sr}$ ). The rear suspension damping coefficient (parameter  $c_{sr}$ ) was left unaltered. The decision whether to increase or decrease the magnitude of the damping coefficient  $c_{sr}$ , needs a clear knowledge of the values of the critical damping constant, the natural frequency and the forcing frequency. In some cases damping can lead to loss of vibration isolation efficiency [7]. Alterations

in parameters of the front suspension system were avoided because making those changes on a motorcycle could largely influence the control behaviour of a whole motorcycle [4].

With the aim of observing how was the vibration behaviour of the model as the position of a seat and hence a rider was changed with respect to the center of gravity, the following two steps were done:

i. In the first approach, the seat was assumed to be exactly located on or above the center of gravity hence the parameter  $a$  was made equal to zero ( $a=0$ ), the simulation was done and the results observed.

ii. The second approach, the value of the parameter  $a$  was made equal to  $L_1$ , this meant that the seat position moved to the rear side such that  $a=L_1$ , the simulation was done and the results observed.

Having performed the simulations and recorded the results, the parameters were returned as at the beginning and a similar procedure was repeated with rear suspension system parameter  $k_{sr}$ . In this case no dimensional alterations were done, but changes were done by reducing the magnitude of a responsible parameter.

#### A. Simulation results after parameter $a$ changes

When the value of  $a$  was changed from  $0.298 \text{ m}$  to  $0$  and then to  $0.595 \text{ m}$  making the model seat position to change with respect to the center of gravity, the displacement and acceleration attained amplitudes was recorded in Tables 2 and 3.

In the first two seconds, the results were fluctuating and unstable, therefore the recorded values were those attained after stabilization. From the simulation results recorded in Table 2 and 3, the following phenomenon was visible. As the position of the seat and hence the rider moved further from the center of gravity location towards the rear wheel, there was a corresponding reduction in the vibration magnitudes of the model component bodies.

**Table 2** Model simulation results: Vibration displacement (meters) of the six bodies composing a model before and after changing the value of parameter  $a$

Variable name	Displacement before parameter change ( $a = 0.298$ )	Displacement after parameter change ( $a = 0$ )	Displacement after parameters change ( $a = 0.595 = L_1$ )
$x_h$	0.044	0.045	0.042
$x_{se}$	0.042	0.045	0.041
$x_b$	0.024	0.025	0.023
$\theta$	0.047	0.056	0.037
$x_{wf}$	0.041	0.044	0.039
$x_{wr}$	0.035	0.039	0.032

**Table 3** Model simulation results: Vibration acceleration ( $m/s^2$ ) of the six bodies composing a model before and after changing the value of parameter  $a$

Variable name	Acceleration before parameter change ( $a = 0.298$ )	Acceleration after parameter change ( $a = 0$ )	Acceleration after parameters change ( $a = 0.595 = L_1$ )
$\ddot{x}_h$	13.223	13.400	12.675
$\ddot{x}_{se}$	12.632	12.850	12.109
$\ddot{x}_b$	07.148	07.410	06.885
$\ddot{\theta}$	13.943	16.640	10.924
$\ddot{x}_{wf}$	12.329	13.070	11.714
$\ddot{x}_{wr}$	10.500	10.525	9.628

**B. Simulation results after parameter  $k_{sr}$  changes**

Stiffness properties of the rear model suspension system ( $k_{sr}$ ) were subject to reduction at random magnitudes. Trials with small values reduction were done, but the simulation results didn't yield notable changes. The decision was made to do big reduction on the parameters for the sake of having notable changes. For consistence it was decided to reduce the parameter values by 10000 N/m. The spring stiffness parameter  $k_{sr}$  was reduced leaving  $c_{sr}$  unchanged. Simulations and observations were done and then the parameter was further reduced by 10000N/m and simulation and observations were repeated. The vibration displacement and acceleration simulation results were recorded in Tables 4 and 5

**Table 4** Model simulation results: Vibration displacement (meters) of the six bodies composing a model before and after reducing parameter  $k_{sr}$

Variable name	Displacement before parameter change ( $k_{sr}=58570$ )	Displacement after $k_{sr}$ parameter first change ( $k_{sr}=48,570$ )	Displacement after $k_{sr}$ parameter second change ( $k_{sr}=38,570$ )
$x_h$	0.044	0.043	0.041
$x_{se}$	0.042	0.041	0.039
$x_b$	0.024	0.023	0.023
$\theta$	0.047	0.046	0.046
$x_{wf}$	0.041	0.041	0.041
$x_{wr}$	0.035	0.035	0.035

From the simulation results in Tables 4 and 5, it was observed that reducing the value of parameter  $k_{sr}$  was accompanied by corresponding decline in both vibration magnitudes (displacement and acceleration), for almost all component bodies of a model except the rear wheel. The changes were more visible in acceleration values than in displacement. From these results it may be said that, stiffness properties of the motorcycle rear suspension system,

is influential on resultant vibration magnitudes as compared to other suspension parameters.

**Table 5** Model simulation results: Vibration acceleration ( $m/s^2$ ) of the six bodies composing a model before and after reducing  $k_{sr}$ .

Variable name	Acceleration before parameter change	Acceleration after $k_{sr}$ parameter change	Acceleration after $c_{sr}$ and $k_{sr}$ parameters change
$\ddot{x}_h$	13.223	12.821	12.263
$\ddot{x}_{se}$	12.632	12.248	11.741
$\ddot{x}_b$	07.148	06.982	06.784
$\ddot{\theta}$	13.943	13.805	13.670
$\ddot{x}_{wf}$	12.329	12.241	12.146
$\ddot{x}_{wr}$	10.500	10.495	10.495

The simulation results in tables 4 and 5 show that out of the five bodies composing a model, the motorcycle body is the part with lowest vibration magnitudes ( $x_b$  and  $\ddot{x}_b$ ), but at the same time the magnitudes due to pitch motion ( $\theta$  and  $\ddot{\theta}$ ) were the highest. Vibration displacement and acceleration for the seat ( $\ddot{x}_{se}$  and  $x_{se}$ ) and those for a rider ( $x_h$  and  $\ddot{x}_h$ ) appeared to be greater even more than those at the wheels (input points). This may have been caused by several factors such as the large value of vibration due to pitch motion, their relative position from the front and rear wheels ( $a$ ,  $L_2$  and  $L_1$ ) and the applied values of the damping constant. High magnitudes of vibration caused by pitch motion were linked to the assumption that the profile of the path was sinusoidal.

**V. CONCLUSIONS**

From the simulation results it may be concluded that

- the location of the rider seat from the centre of gravity of a motorcycle has an influence to the level of vibration magnitude of the rider such that, the farther the rider seat is located from the centre of gravity towards the rear wheel the little the vibration magnitudes of the rider.
- The stiffness of the suspension influences the vibration magnitude of the rider in such a way that the more stiff the suspension the more vibration is transmitted to the rider; hence less stiff suspension is friendlier with regard to vibration exposure.

**VI. RECOMMENDATION**

- In order to achieve the goal of reducing vibration magnitudes of the motorcycle rider caused by the road condition, the following should be put into consideration: Determination of optimum position of the seat relative to the motorcycle body centre of gravity, and rear wheel and applying suspension system which may have variable characteristics (active suspension).

## REFERENCES

1. Abbas,W., Emam,A., Badran, S., Shebl, M., & Aboulatta, O., (2013), Optimal Seat and Suspension Design for a Half-Car with Driver Model Using Genetic Algorithm, *Intelligent Control and Automation, Scientific Research*, 4, pp. 199-205. <http://www.scirp.org/journal/ica>, retrieved on Tuesday 29<sup>th</sup> October, 2013.
2. Ndimila, B.W., Majaja, B.A., Elias, E. and Nalitolela, N.G. (2013), Evaluation of the Extent of Whole Body Vibration Exposure Among Urban Motorcycle Commercial Riders A Case of Dar Es Salaam Commercial Riders, *Year 2013 Annual Roads convention*, Dar es Salaam, Tanzania Roads association.
3. Chen, H.C., Chen, W.C., Liu, Y.P., Chen, C.Y., & Pan, Y. T., (2009), Whole-body Vibration Exposure Experienced by Motorcycle Riders- An evaluation according to ISO 2631-1 and ISO 2631-5 standards, *International Journal of Industrial Ergonomics*, ELSEVIER, 39 (2009) pp707-718.
4. Cossalter,V., Lot,R., and Maggio, F. (2004) The Modal Analysis of a Motorcycle in a straight running and on curve, *Meccanica*, Kluwer Academic Publishers.
5. Cossalter,V., (2006), *Motorcycle Dynamics*, Lulu.com, ISBN978-1-4303-0861-4 <http://books.google.co.tz>, retrieved on Monday 26<sup>th</sup> November 2012
6. Krodkiewsk, J. M., (2008), *Mechanical Vibrations*, Melbourne, Department of Mechanical and Manufacturing Engineering, the University of Melbourne.
7. Rao, S.S., (2007), *Vibration of Continuous Systems*, John Wiley & Sons
8. Satou, Y., Ando, H., Nakiri, M., Nagatomi, K., Yamaguchi, Y., Hashimo, M., Tsuji, Y., Muramoto, J., Mori, M., Hara, K., & Ishitaki, T., (2006), "Effects of Short Term exposure to Whole- Body Vibration on Workfullness level", *Industrial Health*, 2007 No45, Kurume University, Department of Environmental Medicine.
9. Shivakumara, B. S., & Sridhar, V., (2010), "Study on Vibration and its Effect on Health of the Motorcycle rider", *Online Journal of Health and Allied Sciences*, Volume 9 Issue2; Apr-Jun, 2010, Mangalore, south India: ISSN0972-5997 [www.ojhas.org/issue34/2010-2-9.htm](http://www.ojhas.org/issue34/2010-2-9.htm) retrieved on monday19<sup>th</sup> September, 2011.
10. Sharp, R.S., Avangelou, S., & Limebeer, D.J.N.(2004), Advances in the Modeling of Motorcycle Dynamics, *Multibody System Dynamics*, Kluwer Publishers, No 12, pp.251-283.
11. Stotsko, Z. A., Sokil, B.I., & Topilnytsky, V.G., (2007), "Complex Mathematical Model and Optimization of Vibration Volumetric Treatment for Surface of Machine Parts", *Journal of Achievements in Materials and Manufacturing Engineering*, Lvivska Polytechnika, Iviv, Ukraine, Volume 24 issue1 September, 2007, pp,283-290.
12. Wang, W., Rakheja, S. & Boileau, P.E., (2006) 'The role of seat geometry and posture on the mechanical energy absorption characteristics of seated occupants under vertical vibration', *International journal of Industrial Ergonomics* Vol. 36 pp.171-184.