

# Forecasting of a hydropower plant energy production with Fuzzy logic Case for Albania

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**Abstract**—Forecasting of energy production for such small power plants is an essential tool for ensuring ongoing power supply for user demand, planning of reserve power supply and transaction between power plants. Applying several techniques to the datasets we have tried to determine the best method to build a one-step-ahead prediction model. Also we have been aiming to estimate the impact of different attributes on the forecasting process. This paper mainly deals with the design of forecasting model for Hydro power generation using Fuzzy time series. The fuzzy time series has recently received an increasing attention because of its capability of dealing with vague and incomplete data. There have been a variety of models developed either to improve forecasting accuracy or reduce computation overhead. This technique has been applied to forecast various fields and have been shown to forecast better than other models. Hence, in this paper fuzzy time series forecasting technique has been applied on hydro power generation data set. An algorithm is designed and based on the numerical calculations and graphical representations it reveals that Hydro Power generation can be forecasted by using Fuzzy Time Series.

**Keywords**—Fuzzy Logic, Forecasting, HydroPower, time series, energy prediction.

## I. INTRODUCTION

Accurate models for electric power load forecasting are essential to the operation and planning of a utility company. Load forecasting helps an electric utility to make important decisions including decisions on purchasing and generating electric power, load switching, and infrastructure development. One of the most important works of an electric power utility is to correctly predict load requirements.

Energy is considered to be a key point in sustainable economic development and a necessity of a modern life. Sustainable development demands a sustainable supply of energy resources. Renewable energy sources, such as sunlight, wind, geothermal heat, hydropower, etc., are generally related to a sustainable

ones considering relatively long-term periods of time. For example, for large-scale conventional hydroelectric stations (dams) which have water reservoirs electricity production can be flexible since stations turbine systems can be adjusted to adapt to changing energy demand. Energy production of a small and micro hydropower plants depends on the weather conditions like precipitation and temperature. As a result, the energy production of such systems fluctuates and need to be forecasted.

In the last decade, fuzzy time series have received more attention to deal with the vagueness and incompleteness inherent in time series data. Different types of models have been developed either to improve forecasting accuracy or reduce computation overhead. However, the issues of controlling uncertainty in forecasting, effectively partitioning intervals, and

Consistently achieving forecasting accuracy with different interval lengths have been rarely investigated.

Fuzzy set theory and fuzzy logic was first introduced by Zadeh (1965) which provides a general method for handling uncertainty and vagueness in information available in linguistic terms. Song and Chissom (1993) used the fuzzy set theory given by Zadeh to develop models for fuzzy time series forecasting and considered the problem of forecasting enrollments on the time series data of University of Alabama.

### A. Fuzzy Systems:

Fuzzy systems are like expert systems in relaying upon certain rules. These rules here allows fuzzy input. Natural way of behavior of human being are almost fuzzy in all its aspects. Fuzzy systems can solve problems which are difficult for expert systems. It allows the possibility of representation of imprecise human knowledge. Fuzzy systems are based on fuzzy logic which will be discussed in details later on in this paper.

### B. Fuzzy Logic in Power System Operation and Planning:

There is an increasing number of publications on the application of fuzzy logic in the field of power engineering. This shows the potential of this field in

getting better performance of power systems with this logic. There are problems in power systems that contain conflicting objectives. In power systems operation, economy and security, maximum load supply and minimum generating cost are conflicting objectives. The combination of these objectives by weighing coefficients is the traditional approach to solve this problem. Fuzzy theory offers better compromise and obtain solutions which cannot be found by weighing methods. The benefits of fuzzy set theory over traditional methods are as follows:

- It provides alternatives for the many attributes of objective selected.
- It resolves conflicting objectives by designing weights appropriate to a selected objective.
- It provides capability for handling ambiguity expressed in diagnostic process which involves symptoms and causes.
- It develops process control as fuzzy relation between information about the condition of the process to be controlled.
- It develops intelligent robots that employ sensors for path or position determination.
- It improves human reliability models in cases where many people perform multiple tasks.

The areas where fuzzy logic can be used in power Systems cover all the aspects of the power system:

### C. Fuzzy Time Series

In view of making the exposition self-contained, the various definitions and properties of fuzzy time series forecasting found in are summarized and reproduced as:

**Definition 1.** A fuzzy set is a class of objects with a Continuum of grade of membership. Let  $U$  be the Universe of discourse with  $U = \{u_1, u_2, u_3, \dots, u_n\}$

where  $u_i$  are possible linguistic values of  $U$ , then a fuzzy set of linguistic variables  $A_i$  of  $U$  is defined by

$$A_i = \mu_{A_i}(u_1)/u_1 + \mu_{A_i}(u_2)/u_2 + \mu_{A_i}(u_3)/u_3 + \dots + \mu_{A_i}(u_n)/u_n$$

Here  $\mu_{A_i}$  is the membership function of the fuzzy set  $A_i$ , such that  $\mu_{A_i} : U = [0,1]$ .

If  $u_j$  is the member of  $A_i$ , then  $\mu_{A_i}(u_j)$  is the degree of belonging of  $u_j$  to  $A_i$ .

**Definition 2.** Let  $Y(t) (t = \dots, 0, 1, 2, 3, \dots)$ , is a subset of  $R$ , be the universe of discourse on which fuzzy sets  $f_i(t) (i = 1, 2, 3, \dots)$  are defined and  $F(t)$  is collection of  $f_i$ , then  $F(t)$  is defined as fuzzy time series on  $Y(t)$ .

**Definition 3.** Suppose  $F(t)$  is caused only by  $F(t-1)$  and is denoted by  $F(t-1) \rightarrow F(t)$ ; then

there is a fuzzy relationship between  $F(t)$  and  $F(t-1)$  and can be expressed as the fuzzy relational equation:

$$F(t) = F(t-1) \circ R(t, t-1)$$

here “ $\circ$ ” is max-min composition operator. The relation  $R$  is called first-order model of  $F(t)$ . Further, if fuzzy relation  $R(t, t-1)$  of  $F(t)$  is independent of time  $t$ , that is to say for different time  $t_1$  and  $t_2$ ,  $R(t_1, t_1-1) = R(t_2, t_2-1)$  and  $F(t)$  is called a time invariant fuzzy time series.

**Definition 4.** If  $F(t)$  is caused by more fuzzy sets  $F(t-n), F(t-n+1), \dots, F(t-1)$ , the fuzzy relationship is represented by

$$A_{i_1}, A_{i_2}, \dots, A_{i_n} \rightarrow A_j$$

here  $F(t-n) = A_{i_1}, F(t-n+1) = A_{i_2}, \dots, F(t-1) = A_{i_n}$

This relationship is called  $n^{\text{th}}$  order fuzzy time series model.

**Definition 4.** Suppose  $F(t)$  is caused by an  $F(t-1), F(t-2), \dots, \text{and } F(t-m) (m > 0)$  simultaneously and relations are time variant. The  $F(t)$  is said to be time variant fuzzy time series and relation can be expressed as the fuzzy relation equation:

$$F(t) = F(t-1) \circ R^w(t, t-1)$$

Here  $w > 1$  is a time (number of years) parameter by which the forecast  $F(t)$  is being affected. Various complicated computations of relation  $R^w(t, t-1)$ .

## II. STRATEGY OF FUZZY TECHNIQUES BASED TIME SERIES

Below we will look at the forecasting process step by step

We will consider two series:

1. The series of annual production of power consumption by hydropower for the period 2007-2016.
2. The series of monthly production of power consumption by hydropower for the Jan-Dec 2016

**Step1:** initially compute the first order variation of the historical data

**Step2:** Define the universe of discourse,  $U$  based on the range of available variation of the historical data.  $U = [V_{\min} - V1, V_{\max}]$ , where  $V_{\max}$  is the maximum and  $V_{\min}$  value of the first order variation of the data,  $V1$  and  $V2$  are two positive integers so:

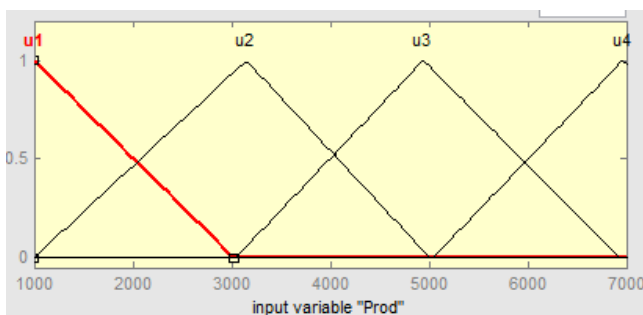
$$U = [V_{\min} - V1, V_{\max} + V1]$$

$$U = [100000, 700000]$$

| Year | Production | First Diff | Fuzzy set |
|------|------------|------------|-----------|
| 2007 | 109,355    | -          | v1        |
| 2008 | 130,569    | 21,214     | v1        |
| 2009 | 168,756    | 38,187     | v1        |
| 2010 | 235,174    | 66,418     | v2        |
| 2011 | 181,479    | (53,695)   | v1        |
| 2012 | 312,159    | 130,680    | v3        |
| 2013 | 401,820    | 89,661     | v4        |
| 2014 | 437,694    | 35,875     | v4        |
| 2015 | 487,109    | 49,415     | v4        |
| 2016 | 661,797    | 174,688    | v6        |

Table 1: The historical data of hydro power

**Step3:** Define Fuzzy sets  $A_i$  on universe of discourse  $U$ . then determine how many linguistic variables to be fuzzy sets.



**Step4:** Fuzzify the variations of the historical data and established the fuzzy logical relationship is represented by  $A_i \rightarrow A_j$  as in table 1.

**Step5:** Regulation of forecasting follows:  $[A_j]$  is corresponding interval  $u_j$  for which membership in  $A_j$  is supremum (i.e.1)  $L [A_j]$  is the length of the interval  $u_j$  for whose membership in  $A_j$  is supremum (i.e.1)  $M [A_j]$  is the mid value of the interval  $u_j$  having supremum membership value in  $A_j$  for a fuzzy logical relationship  $A_i \rightarrow A_j$

- $A_i$  is the fuzzified enrollment of the current year  $n$ ;
- $A_j$  is the fuzzified enrollment of the next year  $n+1$ ;
- $D_i$  is the actual enrollment of the current year  $n$ ;
- $D_{i-1}$  is the actual enrollment of the previous year  $n-1$ ;
- $E_i$  is the variation enrollment of the current year  $n$ ;
- $E_{i-1}$  is the variation enrollment of the previous year  $n-1$ ;

- $F_j$  is the forecasted enrollment of the next year  $n+1$ ;
- (i) Forecasting hydroelectric for the year  $n+1$  is obtained from modified computational algorithm as follows:

Obtain the fuzzy logical relationship  $A_i \rightarrow A_j$ .

If  $E_i < M [A_i]$ , then  $F_j = D_{i-1} + (M [A_j] - 1/4 * L [A_i])$ , Else if  $E_i > M [A_j]$ , then  $F_j = D_{i-1} + (M [A_j] + 1/4 * L [A_i])$ , Else  $F_j = D_{i-1} + M [A_j]$ .

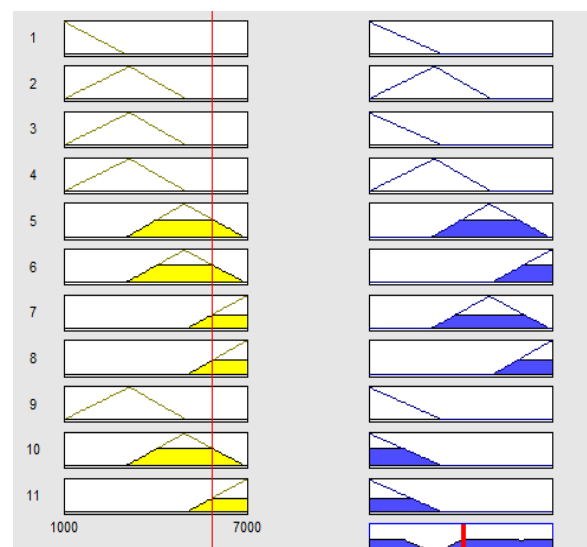
- (ii) Obtain the mean square error is using actual values and forecasted values.

**Step6:** Variations in the Fuzzy Logic Relationships

$$V1 \rightarrow V1; V1 \rightarrow V1; V1 \rightarrow V2; V2 \rightarrow V1; V1 \rightarrow V3; V3 \rightarrow V4; V4 \rightarrow V4; V4 \rightarrow V4; V4 \rightarrow V6;$$

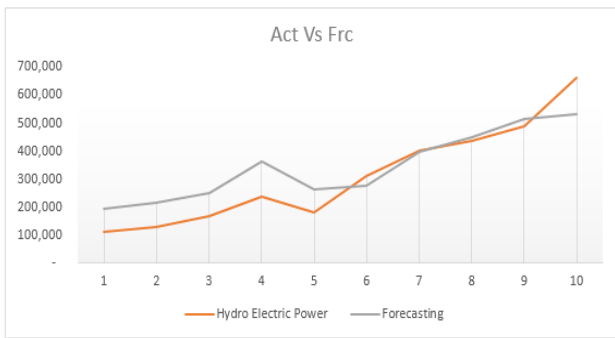
Fuzzy Logic Relationship Groups:

- 1  $V1 \rightarrow V1, V2, V3$
- 2  $V2 \rightarrow V1,$
- 3  $V3 \rightarrow V4$
- 4  $V4 \rightarrow V4, V6$



| Year | Hydro Electric Power | Forecasting | Deviation |
|------|----------------------|-------------|-----------|
| 2007 | 109,355              | 192,000     | 82,645    |
| 2008 | 130,569              | 217,000     | 86,431    |
| 2009 | 168,756              | 252,000     | 83,244    |
| 2010 | 235,174              | 365,000     | 129,826   |
| 2011 | 181,479              | 262,000     | 80,521    |
| 2012 | 312,159              | 277,000     | (35,159)  |
| 2013 | 401,820              | 397,000     | (4,820)   |
| 2014 | 437,694              | 448,000     | 10,306    |
| 2015 | 487,109              | 516,000     | 28,891    |
| 2016 | 661,797              | 534,000     | (127,797) |

Table 2: The historical and forecasting data of Hydro Power plant



Graph 1: The historical and forecasting data

Define the universe of discourse, U based on the range of available variation of the historical data.  $U = [V_{min}-V1, V_{max}]$ , where  $V_{max}$  is the maximum and  $V_{min}$  value of the first order variation of the data, V1 and V2 are two positive integers so:

$$U = [V_{min}-V1, V_{max}+V1]$$

$$U = [10000, 100000]$$

| Month  | Production | First Diff | Fuzzy set |
|--------|------------|------------|-----------|
| Jan-16 | 66,536     |            | V3        |
| Feb-16 | 82,875     | 16,339     | V4        |
| Mar-16 | 91,447     | 8,572      | V5        |
| Apr-16 | 79,733     | (11,713)   | V4        |
| May-16 | 88,496     | 8,763      | V4        |
| Jun-16 | 47,807     | (40,689)   | V2        |
| Jul-16 | 21,481     | (26,326)   | V1        |
| Aug-16 | 13,560     | (7,922)    | V1        |
| Sep-16 | 24,333     | 10,773     | V1        |
| Oct-16 | 45,145     | 20,812     | V2        |
| Nov-16 | 64,561     | 19,416     | V3        |
| Dec-16 | 35,822     | (28,739)   | V4        |

Table 3: The historical data of hydro power

Variations in the Fuzzy Logic Relationships

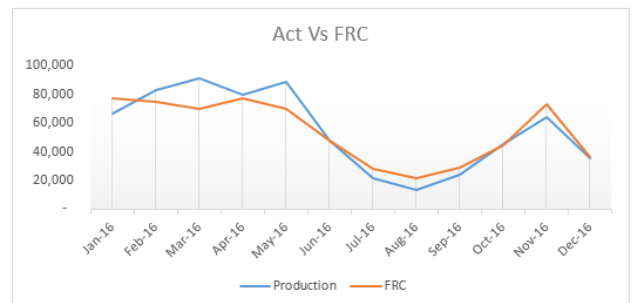
$V3 \rightarrow V4$ ;  $V4 \rightarrow V5$ ;  $V5 \rightarrow V4$ ;  $V4 \rightarrow V4$ ;  $V4 \rightarrow V2$ ;  $V2 \rightarrow V1$ ;  
 $V1 \rightarrow V1$ ;  $V1 \rightarrow V1$ ;  $V1 \rightarrow V2$ ;  $V2 \rightarrow V3$ ;  $V3 \rightarrow V4$ ;

Fuzzy Logic Relationship Groups:

- 1  $V1 \rightarrow V1, V2$ ,
- 2  $V2 \rightarrow V1, V3$
- 3  $V3 \rightarrow V4$
- 4  $V4 \rightarrow V2, V4, V5$
- 5  $V5 \rightarrow V4$ ,

| Month  | Hydro Electric | Forecasting | Deviation |
|--------|----------------|-------------|-----------|
| Jan-16 | 66,536         | 77,100      | 10,564    |
| Feb-16 | 82,875         | 74,800      | (8,075)   |
| Mar-16 | 91,447         | 69,700      | (21,747)  |
| Apr-16 | 79,733         | 77,600      | (2,133)   |
| May-16 | 88,496         | 70,400      | (18,096)  |
| Jun-16 | 47,807         | 47,900      | 93        |
| Jul-16 | 21,481         | 28,100      | 6,619     |
| Aug-16 | 13,560         | 21,300      | 7,740     |
| Sep-16 | 24,333         | 29,400      | 5,067     |
| Oct-16 | 45,145         | 44,800      | (345)     |
| Nov-16 | 64,561         | 73,700      | 9,139     |
| Dec-16 | 35,822         | 36,600      | 778       |

Table 3: The historical and forecasting data of Hydro Power plant



Graph 2: The historical and forecasting data

## I. CONCLUSION

The main objective of this work was to estimate different approaches applied to energy production forecasting for small hydropower plants and determine the best forecasting model analyzing the production of hydropower in Albania, in two series annual production for the years 2007-2016 and monthly production for the period Jan – Dec 2016. Energy production process on a hydropower plant are relevant for building an accurate prediction model. In this paper fuzzy time series method is designed to forecast the hydro power generation of Albania. This work can be extended to develop a method for relating fuzzy logic-linguistic variables with various efficient control of hydropower plant energy in future.

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