# Neural Network Modeling of Concrete Slump and Compressive Strength of a Nigerian Portland Cement

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Bauchi, Nigeria. mni211@yahoo.com relative quantities with the objective of producing, as economic as possible, concrete of certain minimum properties, notably strength, durability, and a required consistency is worked out after which trial mixes are conducted [2]. This process is time consuming, leads to wastage of concrete materials thereby inadvertently increasing cost. It is in view of these shortcomings that this model which employs Artificial Neural Network (ANN) was designed for a selected Portland cement brand.

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The ANN has the ability to learn complex relationships between the inputs and target results and if trained can predict future outcomes when given new data. This paper also intends to provide data which other construction industry workers can use to further broaden the use of this model as its efficiency depends on the quantity if data provided.

# **Neural Network**

The Neural Network (NN) is a toolbox in the MATLAB software. It is a high-performance language for technical computing. It integrates computation, visualization, and programming in an easy-to-use environment where problems and solutions are expressed in familiar mathematical notation. Typical uses include;

- Math Computation,
- Algorithm Development,
- Data Acquisition,
- Modeling, Simulation, and Prototyping,
- Data analysis, Exploration, and Visualizations,
- Scientific and Engineering Graphics,

• Application development, including graphical user interface.

The NN toolbox also includes many kinds of powerful networks for solving problems including;

- Function approximation, modeling,
- Signal processing and prediction,
- Classification and clustering.

These tools are an essential part of many applications, including engineering, finance, medicine, and artificial intelligence (AI).

adjustments to the mix constituents; in most instances this is time consuming and costly. This study is aimed at presenting a model for determining the slump and 28 day compressive strength of fresh and hardened concrete specimens respectively of a Nigerian Portland cement of grade 32.5. The DOE method of mix design was used in predetermining the ratio of materials to be mixed. 36 mix designs were done with 6 cubes casted per each mix (216 concrete cubes in all) of size 100×100×100mm were used in developing the Artificial Neural Network model. The slump of the mix was determined before it was casted. 60% of the samples were randomly selected and used for the training of the Feed-Forward Neural Network while 20% each were used for the testing and validation of the model. The training, testing and validation of the Neural Network were successful. 5 neurons (water content, cement content, coarse aggregate size, coarse aggregate weight and fine aggregate weight) were used in the input layer, 10 and 8 neurons were used in the first and second hidden layers while 2 neurons (slump and compressive strength) were used in the output layer. A learning rate of 0.0001 was used. The network trained after 136 epochs with a Mean Square Error of 0.0134525.

Abstract—Concrete mix designs are usually

succeeded by trial mixes which allow for

Keywords: Concrete Mix, Artificial Neural Network, Training, Neurons, Layers.

# 1. Background

The Nigerian construction industry witness frequent building collapses. This trend has been the foremost concern of the construction industry professionals with the view to curb this trend. Some key factors such as poor supervision, substandard building materials and use of inexperienced workers among others have been identified as the cause of building collapses [1]. In the materials, concrete is most prone to inconsistency when its production is not well supervised.

To achieve concrete of desired quality, a mix design which is defined as the process of selecting suitable ingredients of concrete and determining their

### Artificial Neural Networks (ANN)

Artificial Neural Networks (ANN) was developed to model the human brain. Even a fairly simple and small sized ANN, when compared to the human brain, has some powerful characteristics in knowledge and information processing due to its similarity (to the brain). ANNs can 'learn' complex input-output mappings. The mappings are not specified, but 'learned'. The learning process is used to determine proper interconnection weights, and the network is 'trained' to properly associate the inputs with their corresponding outputs.

An ANN has been described by Tazelaar, [3] as "humanity's attempt to mimic the way the brain does things in order to harness its versatility and ability to infer and intuit from incomplete or confusing information". More specifically, they can be used to learn complex relationships for the recognition of patterns.

An ANN, described in detail by Zurada [4], is first 'trained' to identify the relationship between a series of input vectors and their corresponding output vector. Input vectors are repeatedly presented to the network one at a time, each element of the vector corresponding to a different neuron in the first layer of the network (see Fig. 1)

These inputs are then multiplied by a corresponding weight before being forwarded to every neuron in the next layer of the network. The forwarded values are multiplied by the weights associated with each neuron (see Fig. 2) before being summed together with all other values and sent simultaneously to that neuron.



Figure 1: ANN Architecture



Figure 2: A Neuron

The summed values (one per neuron in the layer) are then forwarded, via a transformation function, to the next layer of the network. The output for the final layer corresponds to the network's calculation as to what the output vector should be. Initially all the weights in the network are set to random values and the network 'learns' by adjusting the weights in such a way as to reduce the difference between the network's calculation of what the output vector should be and the actual value.

After the ANN has been trained it is then tested. Testing involves presenting the network with a series of input vectors for which the tester, but not the network, knows the corresponding output values. The answers given by the network as to what it determines to be the level of output, given the presented input vector, can then be used by the tester to determine the robustness of the training process. If the robustness of the network is deemed sufficient, the network can be used in a truly predictive capacity. NN's are able to solve effectively and efficiently a wide range of problems that are either difficult or impossible to solve using 'conventional' techniques [5].

### Artificial Neuron

An artificial neuron is composed of five main parts: inputs, weights, sum function, activation function and outputs. Inputs are the information that enters the cell from other cells or from the external world. Weights are values that express the effects of an input set or another process element in the previous layer on this process element. Sum function is a function that calculates the net input that comes to a cell [6]. The weighted sums of the input components (net)*j* are calculated by using equation 1:

$$(net)j = \sum_{i=1}^{n} w_{ij}x_i + b \tag{1}$$

Where  $(net)_j$  is the weight of the *j*. neuron for the input received from the preceding layer with *n*. neurons,  $w_{ij}$  is the weight between the *j*. neuron in the preceding layer, *xj* is the output of the *i*. neuron in the preceding layer [7]. *b* is a constant which is an internal addition and  $\Sigma$  represents sum function. The activation function processes the net input obtained from the sum function and determines the cell output. In general for multi-layer receptive models, the sigmoid activation function (*f*(net)) is used. The output of the *j*. neuron (out)*j* is calculated employing Equation 2 with a sigmoid function as follows;

$$(out)j = f(net)j = 1/(1 + e^{-\alpha(net)j})$$
(2)

Where  $\alpha$  is a constant which is used to control the slope of the semi-linear region. The sigmoid non-linearity activates in every layer except in the input layer [6]. The sigmoid function represented by Equation (2) gives inputs in (0, 1). As the sigmoid processor represents a continuous function, it is especially used in non-linear descriptions because its derivatives can be determined easily with regard to the parameters within the (net)*j* variable.

### 2.5 Developing the Neural –Based Model

The basic strategy for developing a neural-based model of material behavior is to train a neural network on the results of a series of experiments on a material (i.e. creating a database of examples). If the experimental results contain the relevant information about the material behavior, then the trained neural network would contain sufficient information about the material behavior to qualify as a material model. Such a trained neural network not only would be able to reproduce the experimental results it was trained on, but through its generalization capability it should be able to approximate the results of other experiments [8].

Most research that used ANN to model material behavior is based on back-propagation networks (BPN). Pala et al (2007) stated that the Back-propagation algorithm is one of the well-known training algorithms for the multi-layer perceptron (MLP); as it is a gradient descent technique which minimizes the error for a particular training pattern in which it adjusts the weighs by a small amount at a time. The BPN learns by comparing its output of each input pattern with a target output of that pattern, then calculating the error and propagating an error function backward through the net.

To run the network after it is trained, the values for the input parameters for the project are presented to the network. The network then calculates the node outputs by using the existing weight values and thresholds developed in the training process. To test the accuracy of the trained network, the coefficient of determination  $R^2$  is adopted. The coefficient is a measure of how well the independent variables took into account the measured dependent variable, and denotes the strength of the linear association between x and v. It is the ratio of the explained variation to the total variation, and such that  $0 < R^2 < 1$ ; the higher the value of R<sup>2</sup>, the better the prediction relation. It is useful, because it gives the proportion of the variance (fluctuation) of one variable that is predictable from the other variable.

# MATERIALS AND METHODS

### Concrete Materials.

The various materials that would be used in the preparation of the concrete specimens are:

-Portland Cement (Grade 32.5)

-Coarse aggregates of size 10mm and 20mm obtained from a quarry site. The aggregates were cubical in shape.

-Fine Aggregate: river sand which is free from organic materials and clay particles was used.

-Water: clean and drinkable water was used for the mix.

Mix Design:

The DOE Method of Concrete Mix Design was used to ascertain the proportions of materials in the mixes to be prepared. The method is applicable to concrete for most purposes, including roads. The method has been used for designing concrete containing fly ash (FA), or granulated blast furnace slag (GGBS).

Weight batching was used while the mixing was done by hand. Compaction of the samples was attained by tamping the moulds in a uniform specified manner.

### **Developing the Feed Forward Neural Network**

In developing the Neural Network for compressive strength and slump prediction, the following parameters were used as input data; size of aggregate (SA), weight of cement (C), weight of water (W), weight of sand (S), and weight of crushed stone (CS). The quantities of the materials were varied to determine their resultant effect on the slump and compressive strength of the resulting concrete after curing by immersion for 28days. Minimum and maximum values of the constituent materials were determined from the mix design.

The input layer consisted of 5 (five) inputs while the output layer consisted of two outputs; namely, compressive strength and slump. The other parameters needed in the model development included; number of hidden layers, number of neurons in hidden layers and learning rate were determined as the model was simulated.

### Sample Size

A total of 216 (100×100×100mm size) cubes of concrete were casted and used in the training, testing and validation of the model. 60% of the data was randomly selected and used for the training while 20% each were used for the testing and validation of the model.

### **RESULTS AND DISCUSSION**

### **Concrete Slump and Compressive Strengths:**

The concrete produced had varying water/cement ratios thereby leading to varying slumps and compressive strengths. The slumps varied from 0 to 130 while the compressive strength of the samples was between 11- 30N/mm<sup>2</sup>.

# Training, Testing and Validation of Specimen Data:

The network was successfully trained. The Mean Square Error (MSE) obtained after the training of the network was 0.0134525. Other parameters used were a learning rate of 0.0001, performance goal of 0, number of training epochs was set at 10,000, while the epoch shows was set to 10. The transfer function used between the first (i.e. input layer), second and third layers was the 'tansigmoid' function while the 'purelin' transfer function was used between the third and fourth layer (i.e. output layer). The input and output vector data were divided as follows; 60 per cent was used to train the network, 20 per cent was

used to validate how well the network generalized, while the last 20 per cent of the vectors provided an independent test of the network generalization to data that the network has never seen. The Scaled Conjugate Gradient algorithm ('trainscg') was used to train the feed forward network. In order to make the training process more efficient, the input and output data were preprocessed and scaled. The data were normalized by scaling the input and targets vectors using the mean and standard deviations of the training set. The function *mapstd* was used to normalize and scale the inputs and targets so that they had zero mean and unity standard deviation. The normalized inputs and targets were stored in matrices pn and tn which returned values of zero means and unity standard deviation. The settings structure ps and ts contained the means and standard deviations of the original inputs and original targets after which a Principal Component Analysis (PCA) was conducted on the input and output vectors.

With **mapstd** being used to scale the targets, the output of the network was trained to produce outputs with zero mean and unity standard deviation. Inorder to convert these outputs back into the same units that were used for the original targets, **ts** was used. The following code was used to simulate the network that was trained, and used to convert the network output back to its original units.

### an = sim(net,pn);

### a = mapstd('reverse',an,ts);

The network output **an** corresponds to the normalized targets **tn** while the unnormalized network output **a** had the same units as the original targets **t**. Since **mapstd** was used to preprocess the training data set, whenever the trained network is to be used with new inputs, the data should be preprocessed with the means and standard deviations that were computed for the training set using **ps**.

### CONCLUSION

The code used for the NN are shown in Appendix A while Appendix B is a table which shows the network inputs, targets and predicted outcomes from the model.

The following code can be employed when new set of inputs are to be introduced to the already trained network.

### pnewn = mapstd(`apply',pnew,ps);

#### anewn = sim(net,pnewn);

### anew = mapstd(`reverse',anewn,ts);

The following graphs and plots were also obtained after the neural network was trained.







Figure 4: Slump: Validation Set against Target Outputs of Concrete Slumps.



Figure 5: Training Set against Target Outputs of Compressive Strengths



Figure 6: Comparison of Actual and Predicted Slump (mm)



Figure 7: Comparison of Actual and Predicted Compressive Strength (N/mm<sup>2</sup>).

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# APPENDIX

# A. MATLAB Code used in Training Neural Network.

>> B = [180 180 180 180 180 180 180 205 205 205 205 205 205 230 230 230 230 230 230 250 250 250 250 250 180 180 180 180 180 180 205 205 205 205 205 205 230 230 230 230 230 230 250 250 250 250 250 250 180 180 180 180 180 180 205 205 205 205 205 205 230 230 230 230 230 230 250 250 250 250 250 250 180 180 180 180 180 180 205 205 205 205 205 205 230 230 230 230 230 230 250 250 250 205 205 205 230 230 230 230 230 230 250 250 250 205 205 205 205 230 230 230 230 230 230 250 250 250 >> C = [225 225 225 225 225 225 256 256 256 256 256 256 288 288 288 288 288 288 288 313 313 313 313 313 313 247 247 247 247 247 247 247 281 281 281 281 281 281 315 315 315 315 315 315 315 342 342 342 342 342 342 277 277 277 277 277 277 277 315 315 315 315 315 315 354 354 354 354 354 354 354 385 385 385 385 385 385 300 300 300 300 300 300 342 342 342 342 342 342 383 383 383 383 383 383 383 417 417 417 373 373 373 418 418 418 418 418 418 418 455 455 455 455 455 455 180 180 180 180 180 180 238 238 238 238 238 238 263 263 263 263 263 263 263 281 281 281 281 281 281 275 275 275 275 275 275 292 292 292 292 292 292 323 323 323 323 323 323 346 346 346 346 346 346 300 300 300 300 300 300 317 317 317 317 317 317 350 350 350 350 350 350 375 375 375 352 352 352 389 389 389 389 389 389 417 417 417 417 417 417];

>> D = [818 818 818 818 818 818 818 853 853 853 894 894 894 809 809 809 809 809 809 785 785 785 771 771 771 804 804 804 804 804 804 804 815 815 815 815 815 815 749 749 749 749 749 749 749 723 723 723 723 723 723 773 773 773 773 773 773 808 808 808 808 808 808 699 699 699 699 699 699 711 711 711 711 711 711 775 775 775 775 775 775 806 806 806 806 806 806 742 742 742 742 742 742 742 708 708 708 708 708 708 732 732 732 732 732 732 732 825 825 825 825 825 825 608 608 608 608 608 608 610 610 610 610 610 610 654 654 654 654 654 654 706 706 706 706 706 706 600 600 600 600 600 600 602 602 602 694 694 694 553 553 553 553 553 553 572 572 572 572 572 572 594 594 594 594 594 594 678 678 678 678 678 678];

 >> p = vertcat(A,B,C,D,E);

>> G = [12 12 13 13 12 13 13 14 14 14 13 13 11 13 12 12 11 12 12 13 12 13 13 13 12 12 12 12 13 13 12 16 15 19 19 18 18 15 15 17 17 16 17 15 16 16 15 17 15 20 20 18 19 18 20 21 21 22 22 22 22 20 21 22 22 20 19 20 19 21 19 20 21 19 17 18 18 19 20 25 24 25 24 25 25 25 25 24 27 25 26 17 16 17 17 15 18 26 26 25 25 26 26 24 25 27 25 24 25 23 23 24 24 26 25 24 24 23 23 24 24 12 13 12 13 12 13 17 17 17 17 17 16 16 16 16 17 16 14 14 14 15 14 13 25 24 25 24 24 24 24 24 24 24 23 24 16 15 16 17 17 17 19 18 18 19 19 21 25 25 25 25 25 25 25 21 21 22 21 21 22 22 23 20 22 22 22 22 22 22 22 22 27 27 26 26 27 26 27 26 26 26 26 26 29 29 29 29 29 28 30 30 29 30 29 30];

- >> t = vertcat(F,G);>> [pn,pp1] = mapstd (p); >> [tn,tp] = mapstd (t); >> [ptrans,pp2] = processpca (pn,0.001); >> [R,Q] = size (ptrans); >> iitst = 2:4:Q: >> iival = 4:4:Q: >> iitr = [1:4:Q 3:4:Q]; >> validation.P = ptrans (:,iival); >> validation.T = tn (:,iival); >> testing.P = ptrans (:,iitst); >> testing.T = tn (:,iitst); >> ptr = ptrans (:,iitr); >> ttr = tn (:,iitr); >> net = newff(minmax(ptr),[10 8 2],{'tansig' 'tansig' 'purelin'}, 'trainscg'); >> net.trainParam.show = 10; >> net.trainParam.lr = 0.0001; >> net.trainParam.epochs = 10000;
  - >> net.trainParam.goal = 0;
  - >> [net,tr] = train(net,ptr,ttr,[],[],validation,testing);

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A = Coarse Aggregate Size, B = Water Content (g), C = Cement Content (g), D = Fine Aggregate Weight (g), E = Coarse Aggregate Weight (g), F = Experimental Slump Values (mm), G = Experimental Compressive Strength (N/mm<sup>2</sup>), H = Predicted Slump Values (mm), J = Predicted Compressive Strength Values (N/mm<sup>2</sup>).

B. Network Inputs, Targets And Predicted Outcomes From The Model

|     |    |     |     |     |      |     |    |    |    | 2 | +0              | 10 | 200        | 342        | 044        |
|-----|----|-----|-----|-----|------|-----|----|----|----|---|-----------------|----|------------|------------|------------|
| S/N | А  | В   | С   | D   | Е    | F   | G  | Н  | J  | 2 | 46              | 10 | 250        | 342        | 844        |
| 1   | 10 | 180 | 225 | 818 | 1227 | 0   | 12 | -2 | 12 | 4 | 47 ·            | 10 | 250        | 342        | 844        |
| 2   | 10 | 180 | 225 | 818 | 1227 | 0   | 12 | -2 | 12 | 2 | 48 <sup>-</sup> | 10 | 250        | 342        | 844        |
| 3   | 10 | 180 | 225 | 818 | 1227 | 0   | 13 | -2 | 12 | 4 | 49 <sup>-</sup> | 10 | 180        | 277        | 777        |
| 4   | 10 | 180 | 225 | 818 | 1227 | 0   | 13 | -2 | 12 | Ę | 50 <sup>-</sup> | 10 | 180        | 277        | 777        |
| 5   | 10 | 180 | 225 | 818 | 1227 | 0   | 12 | -2 | 12 | Ę | 51              | 10 | 180        | 277        | 777        |
| 6   | 10 | 180 | 225 | 818 | 1227 | 0   | 13 | -2 | 12 | Ę | 52              | 10 | 180        | 277        | 777        |
| 7   | 10 | 205 | 256 | 853 | 1086 | 0   | 13 | 3  | 14 | Ę | 53              | 10 | 180        | 277        | 777        |
| 8   | 10 | 205 | 256 | 853 | 1086 | 0   | 14 | 3  | 14 | Ę | 54              | 10 | 180        | 277        | 777        |
| 9   | 10 | 205 | 256 | 853 | 1086 | 0   | 14 | 3  | 14 | Ę | 55              | 10 | 205        | 315        | 771        |
| 10  | 10 | 205 | 256 | 853 | 1086 | 0   | 14 | 3  | 14 | Ę | 56 <sup>-</sup> | 10 | 205        | 315        | 771        |
| 11  | 10 | 205 | 256 | 853 | 1086 | 0   | 13 | 3  | 14 | Ę | 57              | 10 | 205        | 315        | 771        |
| 12  | 10 | 205 | 256 | 853 | 1086 | 0   | 13 | 3  | 14 | Ę | 58 <sup>-</sup> | 10 | 205        | 315        | 771        |
| 13  | 10 | 230 | 288 | 889 | 963  | 40  | 11 | 36 | 12 | Ę | 59 <sup>-</sup> | 10 | 205        | 315        | /71        |
| 14  | 10 | 230 | 288 | 889 | 963  | 40  | 13 | 36 | 12 | 6 | 00 °            | 10 | 205        | 315        | //1        |
| 15  | 10 | 230 | 288 | 889 | 963  | 40  | 12 | 36 | 12 | 6 | 01 (<br>20 -    | 10 | 230        | 354        | 804        |
| 16  | 10 | 230 | 288 | 889 | 963  | 40  | 12 | 36 | 12 | ť | o∠ ′            | 10 | ∠30<br>220 | 304<br>351 | 804<br>804 |
| 17  | 10 | 230 | 288 | 889 | 963  | 40  | 11 | 36 | 12 |   | 55<br>54        | 10 | ∠30<br>220 | 354        | 004<br>804 |
| 18  | 10 | 230 | 288 | 889 | 963  | 40  | 12 | 36 | 12 | 6 | 54<br>35        | 10 | 230        | 354        | 804<br>804 |
| 19  | 10 | 250 | 313 | 894 | 894  | 100 | 12 | 99 | 12 | ĥ | 56 ·            | 10 | 230        | 354        | 804        |
| 20  | 10 | 250 | 313 | 894 | 894  | 100 | 13 | 99 | 12 | f | 57 ·            | 10 | 250        | 385        | 815        |
| 21  | 10 | 250 | 313 | 894 | 894  | 100 | 12 | 99 | 12 | e | 58 <sup>-</sup> | 10 | 250        | 385        | 815        |
| 22  | 10 | 250 | 313 | 894 | 894  | 100 | 13 | 99 | 12 | 6 | 69 <sup>-</sup> | 10 | 250        | 385        | 815        |
| 23  | 10 | 250 | 313 | 894 | 894  | 100 | 13 | 99 | 12 | - | 70 <sup>-</sup> | 10 | 250        | 385        | 815        |
| 24  | 10 | 250 | 313 | 894 | 894  | 100 | 13 | 99 | 12 | 7 | 71 <sup>·</sup> | 10 | 250        | 385        | 815        |
| 25  | 10 | 180 | 247 | 809 | 1214 | 0   | 12 | -3 | 13 | 7 | 72 <sup>-</sup> | 10 | 250        | 385        | 815        |
| 26  | 10 | 180 | 247 | 809 | 1214 | 0   | 12 | -3 | 13 | 7 | 73              | 10 | 180        | 300        | 749        |
| 27  | 10 | 180 | 247 | 809 | 1214 | 0   | 12 | -3 | 13 | 7 | 74 <sup>-</sup> | 10 | 180        | 300        | 749        |
| 28  | 10 | 180 | 247 | 809 | 1214 | 0   | 13 | -3 | 13 | 7 | 75 <sup>-</sup> | 10 | 180        | 300        | 749        |
| 29  | 10 | 180 | 247 | 809 | 1214 | 0   | 13 | -3 | 13 | 7 | 76 <sup>-</sup> | 10 | 180        | 300        | 749        |
| 30  | 10 | 180 | 247 | 809 | 1214 | 0   | 12 | -3 | 13 | 7 | 77              | 10 | 180        | 300        | 749        |
| 31  | 10 | 205 | 281 | 785 | 1129 | 10  | 16 | 11 | 18 | 7 | 78              | 10 | 180        | 300        | 749        |
| 32  | 10 | 205 | 281 | 785 | 1129 | 10  | 15 | 11 | 18 | 7 | 79 <sup>-</sup> | 10 | 205        | 342        | 723        |
| 33  | 10 | 205 | 281 | 785 | 1129 | 10  | 19 | 11 | 18 | 8 | 30 <sup>·</sup> | 10 | 205        | 342        | 723        |
| 34  | 10 | 205 | 281 | 785 | 1129 | 10  | 19 | 11 | 18 | 3 | 31 <sup>-</sup> | 10 | 205        | 342        | 723        |
| 35  | 10 | 205 | 281 | 785 | 1129 | 10  | 18 | 11 | 18 | } | 32 <sup>·</sup> | 10 | 205        | 342        | 723        |
| 36  | 10 | 205 | 281 | 785 | 1129 | 10  | 18 | 11 | 18 | 3 | 33 '            | 10 | 205        | 342        | 723        |
| 37  | 10 | 230 | 315 | 858 | 967  | 40  | 15 | 46 | 16 | 5 | 54 '<br>55 -    | 10 | 205        | 342        | 723        |
|     |    |     |     |     |      |     |    |    |    | 8 | 35 '            | 10 | 230        | 383        | 113        |

| 38 | 10 | 230 | 315 | 858 | 967  | 40  | 15 | 46  | 16 |  |
|----|----|-----|-----|-----|------|-----|----|-----|----|--|
| 39 | 10 | 230 | 315 | 858 | 967  | 40  | 17 | 46  | 16 |  |
| 40 | 10 | 230 | 315 | 858 | 967  | 40  | 17 | 46  | 16 |  |
| 41 | 10 | 230 | 315 | 858 | 967  | 40  | 16 | 46  | 16 |  |
| 42 | 10 | 230 | 315 | 858 | 967  | 40  | 17 | 46  | 16 |  |
| 43 | 10 | 250 | 342 | 844 | 914  | 100 | 15 | 102 | 16 |  |
| 44 | 10 | 250 | 342 | 844 | 914  | 100 | 16 | 102 | 16 |  |
| 45 | 10 | 250 | 342 | 844 | 914  | 100 | 16 | 102 | 16 |  |
| 46 | 10 | 250 | 342 | 844 | 914  | 100 | 15 | 102 | 16 |  |
| 47 | 10 | 250 | 342 | 844 | 914  | 100 | 17 | 102 | 16 |  |
| 48 | 10 | 250 | 342 | 844 | 914  | 100 | 15 | 102 | 16 |  |
| 49 | 10 | 180 | 277 | 777 | 1216 | 0   | 20 | 1   | 17 |  |
| 50 | 10 | 180 | 277 | 777 | 1216 | 0   | 20 | 1   | 17 |  |
| 51 | 10 | 180 | 277 | 777 | 1216 | 0   | 18 | 1   | 17 |  |
| 52 | 10 | 180 | 277 | 777 | 1216 | 0   | 19 | 1   | 17 |  |
| 53 | 10 | 180 | 277 | 777 | 1216 | 0   | 18 | 1   | 17 |  |
| 54 | 10 | 180 | 277 | 777 | 1216 | 0   | 20 | 1   | 17 |  |
| 55 | 10 | 205 | 315 | 771 | 1109 | 5   | 21 | 6   | 20 |  |
| 56 | 10 | 205 | 315 | 771 | 1109 | 5   | 21 | 6   | 20 |  |
| 57 | 10 | 205 | 315 | 771 | 1109 | 5   | 22 | 6   | 20 |  |
| 58 | 10 | 205 | 315 | 771 | 1109 | 5   | 22 | 6   | 20 |  |
| 59 | 10 | 205 | 315 | 771 | 1109 | 5   | 22 | 6   | 20 |  |
| 60 | 10 | 205 | 315 | 771 | 1109 | 5   | 22 | 6   | 20 |  |
| 61 | 10 | 230 | 354 | 804 | 982  | 60  | 20 | 54  | 21 |  |
| 62 | 10 | 230 | 354 | 804 | 982  | 60  | 21 | 54  | 21 |  |
| 63 | 10 | 230 | 354 | 804 | 982  | 60  | 22 | 54  | 21 |  |
| 64 | 10 | 230 | 354 | 804 | 982  | 60  | 22 | 54  | 21 |  |
| 65 | 10 | 230 | 354 | 804 | 982  | 60  | 20 | 54  | 21 |  |
| 66 | 10 | 230 | 354 | 804 | 982  | 60  | 19 | 54  | 21 |  |
| 67 | 10 | 250 | 385 | 815 | 900  | 150 | 20 | 145 | 21 |  |
| 68 | 10 | 250 | 385 | 815 | 900  | 150 | 19 | 145 | 21 |  |
| 69 | 10 | 250 | 385 | 815 | 900  | 150 | 21 | 145 | 21 |  |
| 70 | 10 | 250 | 385 | 815 | 900  | 150 | 19 | 145 | 21 |  |
| 71 | 10 | 250 | 385 | 815 | 900  | 150 | 20 | 145 | 21 |  |
| 72 | 10 | 250 | 385 | 815 | 900  | 150 | 21 | 145 | 21 |  |
| 73 | 10 | 180 | 300 | 749 | 1221 | 5   | 19 | 3   | 20 |  |
| 74 | 10 | 180 | 300 | 749 | 1221 | 5   | 17 | 3   | 20 |  |
| 75 | 10 | 180 | 300 | 749 | 1221 | 5   | 18 | 3   | 20 |  |
| 76 | 10 | 180 | 300 | 749 | 1221 | 5   | 18 | 3   | 20 |  |
| 77 | 10 | 180 | 300 | 749 | 1221 | 5   | 19 | 3   | 20 |  |
| 78 | 10 | 180 | 300 | 749 | 1221 | 5   | 20 | 3   | 20 |  |
| 79 | 10 | 205 | 342 | 723 | 1130 | 20  | 25 | 9   | 25 |  |
| 80 | 10 | 205 | 342 | 723 | 1130 | 20  | 24 | 9   | 25 |  |
| 81 | 10 | 205 | 342 | 723 | 1130 | 20  | 25 | 9   | 25 |  |
| 82 | 10 | 205 | 342 | 723 | 1130 | 20  | 24 | 9   | 25 |  |
| 83 | 10 | 205 | 342 | 723 | 1130 | 20  | 25 | 9   | 25 |  |

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|---|----|---|-----|-----|------|-----|----|-----|----|-----|----|---|-----|-----|---|---|----|---|----|
| 86  | 10 | 230   | 383 | 773 | 984  | 50  | 25 | 55  | 24 | 134 | 20 | 210   | 263 | 732 | 1195  | 50  | 16 | 51  | 16 |
| 87  | 10 | 230   | 383 | 773 | 984  | 50  | 24 | 55  | 24 | 135 | 20 | 210   | 263 | 732 | 1195  | 50  | 16 | 51  | 16 |
| 88  | 10 | 230   | 383 | 773 | 984  | 50  | 27 | 55  | 24 | 136 | 20 | 210   | 263 | 732 | 1195  | 50  | 16 | 51  | 16 |
| 89  | 10 | 230   | 383 | 773 | 984  | 50  | 25 | 55  | 24 | 137 | 20 | 210   | 263 | 732 | 1195  | 50  | 17 | 51  | 16 |
| 90  | 10 | 230   | 383 | 773 | 984  | 50  | 26 | 55  | 24 | 138 | 20 | 210   | 263 | 732 | 1195  | 50  | 16 | 51  | 16 |
| 91  | 10 | 250   | 417 | 808 | 875  | 100 | 17 | 100 | 17 | 139 | 20 | 225   | 281 | 825 | 1049  | 110   | 14 | 112   | 14 |
| 92  | 10 | 250   | 417 | 808 | 875  | 100 | 16 | 100 | 17 | 140 | 20 | 225   | 281 | 825 | 1049  | 110   | 14 | 112   | 14 |
| 93  | 10 | 250   | 417 | 808 | 875  | 100 | 17 | 100 | 17 | 141 | 20 | 225   | 281 | 825 | 1049  | 110   | 14 | 112   | 14 |
| 94  | 10 | 250   | 417 | 808 | 875  | 100 | 17 | 100 | 17 | 142 | 20 | 225   | 281 | 825 | 1049  | 110   | 15 | 112   | 14 |
| 95  | 10 | 250   | 417 | 808 | 875  | 100 | 15 | 100 | 17 | 143 | 20 | 225   | 281 | 825 | 1049  | 110   | 14 | 112   | 14 |
| 96  | 10 | 250   | 417 | 808 | 875  | 100 | 18 | 100 | 17 | 144 | 20 | 225   | 281 | 825 | 1049  | 110   | 13 | 112   | 14 |
| 97  | 10 | 180   | 327 | 699 | 1244 | 0   | 26 | 8   | 25 | 145 | 20 | 170   | 275 | 608 | 1417  | 0   | 25 | 4   | 24 |
| 98  | 10 | 180   | 327 | 699 | 1244 | 0   | 26 | 8   | 25 | 146 | 20 | 170   | 275 | 608 | 1417  | 0   | 24 | 4   | 24 |
| 99  | 10 | 180   | 327 | 699 | 1244 | 0   | 25 | 8   | 25 | 147 | 20 | 170   | 275 | 608 | 1417  | 0   | 25 | 4   | 24 |
| 100   | 10 | 180   | 327 | 699 | 1244 | 0   | 25 | 8   | 25 | 148 | 20 | 170   | 275 | 608 | 1417  | 0   | 24 | 4   | 24 |
| 101   | 10 | 180   | 327 | 699 | 1244 | 0   | 26 | 8   | 25 | 149 | 20 | 170   | 275 | 608 | 1417  | 0   | 24 | 4   | 24 |
| 102   | 10 | 180   | 327 | 699 | 1244 | 0   | 26 | 8   | 25 | 150 | 20 | 170   | 275 | 608 | 1417  | 0   | 24 | 4   | 24 |
| 103   | 10 | 205   | 373 | 711 | 1111 | 5   | 24 | 5   | 25 | 151 | 20 | 190   | 292 | 610 | 1358  | 5   | 24 | 5   | 24 |
| 104   | 10 | 205   | 373 | 711 | 1111 | 5   | 25 | 5   | 25 | 152 | 20 | 190   | 292 | 610 | 1358  | 5   | 24 | 5   | 24 |
| 105   | 10 | 205   | 373 | 711 | 1111 | 5   | 27 | 5   | 25 | 153 | 20 | 190   | 292 | 610 | 1358  | 5   | 24 | 5   | 24 |
| 106   | 10 | 205   | 373 | 711 | 1111 | 5   | 25 | 5   | 25 | 154 | 20 | 190   | 292 | 610 | 1358  | 5   | 24 | 5   | 24 |
| 107   | 10 | 205   | 373 | 711 | 1111 | 5   | 24 | 5   | 25 | 155 | 20 | 190   | 292 | 610 | 1358  | 5   | 23 | 5   | 24 |
| 108   | 10 | 205   | 373 | 711 | 1111 | 5   | 25 | 5   | 25 | 156 | 20 | 190   | 292 | 610 | 1358  | 5   | 24 | 5   | 24 |
| 109   | 10 | 230   | 418 | 775 | 947  | 50  | 23 | 51  | 25 | 157 | 20 | 210   | 323 | 654 | 1213  | 60  | 16 | 66  | 16 |
| 110   | 10 | 230   | 418 | 775 | 947  | 50  | 23 | 51  | 25 | 158 | 20 | 210   | 323 | 654 | 1213  | 60  | 15 | 66  | 16 |
| 111   | 10 | 230   | 418 | 775 | 947  | 50  | 24 | 51  | 25 | 159 | 20 | 210   | 323 | 654 | 1213  | 60  | 16 | 66  | 16 |
| 112   | 10 | 230   | 418 | 775 | 947  | 50  | 24 | 51  | 25 | 160 | 20 | 210   | 323 | 654 | 1213  | 60  | 17 | 66  | 16 |
| 113   | 10 | 230   | 418 | 775 | 947  | 50  | 26 | 51  | 25 | 161 | 20 | 210   | 323 | 654 | 1213  | 60  | 17 | 66  | 16 |
| 114   | 10 | 230   | 418 | 775 | 947  | 50  | 25 | 51  | 25 | 162 | 20 | 210   | 323 | 654 | 1213  | 60  | 17 | 66  | 16 |
| 115   | 10 | 250   | 455 | 806 | 839  | 90  | 24 | 88  | 24 | 163 | 20 | 225   | 346 | 706 | 1103  | 110   | 19 | 111   | 19 |
| 116   | 10 | 250   | 455 | 806 | 839  | 90  | 24 | 88  | 24 | 164 | 20 | 225   | 346 | 706 | 1103  | 110   | 18 | 111   | 19 |
| 117   | 10 | 250   | 455 | 806 | 839  | 90  | 23 | 88  | 24 | 165 | 20 | 225   | 346 | 706 | 1103  | 110   | 18 | 111   | 19 |
| 118   | 10 | 250   | 455 | 806 | 839  | 90  | 23 | 88  | 24 | 166 | 20 | 225   | 346 | 706 | 1103  | 110   | 19 | 111   | 19 |
| 119   | 10 | 250   | 455 | 806 | 839  | 90  | 24 | 88  | 24 | 167 | 20 | 225   | 346 | 706 | 1103  | 110   | 19 | 111   | 19 |
| 120   | 10 | 250   | 455 | 806 | 839  | 90  | 24 | 88  | 24 | 168 | 20 | 225   | 346 | 706 | 1103  | 110   | 21 | 111   | 19 |
| 121   | 20 | 170   | 180 | 742 | 1378 | 0   | 12 | -2  | 12 | 169 | 20 | 170   | 300 | 600 | 1400  | 0   | 25 | 1   | 25 |
| 122   | 20 | 170   | 180 | 742 | 1378 | 0   | 13 | -2  | 12 | 170 | 20 | 170   | 300 | 600 | 1400  | 0   | 25 | 1   | 25 |
| 123   | 20 | 170   | 180 | 742 | 1378 | 0   | 12 | -2  | 12 | 171 | 20 | 170   | 300 | 600 | 1400  | 0   | 25 | 1   | 25 |
| 124   | 20 | 170   | 180 | 742 | 1378 | 0   | 13 | -2  | 12 | 172 | 20 | 170   | 300 | 600 | 1400  | 0   | 25 | 1   | 25 |
| 125   | 20 | 170   | 180 | 742 | 1378 | 0   | 12 | -2  | 12 | 173 | 20 | 170   | 300 | 600 | 1400  | 0   | 25 | 1   | 25 |
| 126   | 20 | 170   | 180 | 742 | 1378 | 0   | 13 | -2  | 12 | 174 | 20 | 170   | 300 | 600 | 1400  | 0   | 25 | 1   | 25 |
| 127   | 20 | 190   | 238 | 708 | 1314 | 15  | 17 | 15  | 17 | 175 | 20 | 190   | 317 | 602 | 1341  | 0   | 21 | 0   | 21 |
| 128   | 20 | 190   | 238 | 708 | 1314 | 15  | 17 | 15  | 17 | 176 | 20 | 190   | 317 | 602 | 1341  | 0   | 21 | 0   | 21 |
| 129   | 20 | 190   | 238 | 708 | 1314 | 15  | 17 | 15  | 17 | 177 | 20 | 190   | 317 | 602 | 1341  | 0   | 22 | 0   | 21 |
| 130   | 20 | 190   | 238 | 708 | 1314 | 15  | 17 | 15  | 17 | 178 | 20 | 190   | 317 | 602 | 1341  | 0   | 21 | 0   | 21 |
| 131   | 20 | 190   | 238 | 708 | 1314 | 15  | 17 | 15  | 17 | 179 | 20 | 190   | 317 | 602 | 1341  | 0   | 21 | 0   | 21 |
| 132   | 20 | 190   | 238 | 708 | 1314 | 15  | 17 | 15  | 17 | 180 | 20 | 190   | 317 | 602 | 1341  | 0   | 22 | 0   | 21 |
| 133   | 20 | 210   | 263 | 732 | 1195 | 50  | 16 | 51  | 16 | 181 | 20 | 225   | 346 | 706 | 1103  | 110   | 19 | 103   | 22 |

| 182 | 20 | 225 | 346 | 706 | 1103 | 110 | 18 | 103 | 22 |
|-----|----|-----|-----|-----|------|-----|----|-----|----|
| 183 | 20 | 225 | 346 | 706 | 1103 | 110 | 18 | 103 | 22 |
| 184 | 20 | 225 | 346 | 706 | 1103 | 110 | 19 | 103 | 22 |
| 185 | 20 | 225 | 346 | 706 | 1103 | 110 | 19 | 103 | 22 |
| 186 | 20 | 225 | 346 | 706 | 1103 | 110 | 21 | 103 | 22 |
| 187 | 20 | 170 | 300 | 600 | 1400 | 0   | 25 | 111 | 22 |
| 188 | 20 | 170 | 300 | 600 | 1400 | 0   | 25 | 111 | 22 |
| 189 | 20 | 170 | 300 | 600 | 1400 | 0   | 25 | 111 | 22 |
| 190 | 20 | 170 | 300 | 600 | 1400 | 0   | 25 | 111 | 22 |
| 191 | 20 | 170 | 300 | 600 | 1400 | 0   | 25 | 111 | 22 |
| 192 | 20 | 170 | 300 | 600 | 1400 | 0   | 25 | 111 | 22 |
| 193 | 20 | 190 | 317 | 602 | 1341 | 0   | 21 | -2  | 27 |
| 194 | 20 | 190 | 317 | 602 | 1341 | 0   | 21 | -2  | 27 |
| 195 | 20 | 190 | 317 | 602 | 1341 | 0   | 22 | -2  | 27 |
| 196 | 20 | 190 | 317 | 602 | 1341 | 0   | 21 | -2  | 27 |
| 197 | 20 | 190 | 317 | 602 | 1341 | 0   | 21 | -2  | 27 |
| 198 | 20 | 190 | 317 | 602 | 1341 | 0   | 22 | -2  | 27 |
| 199 | 20 | 190 | 352 | 572 | 1336 | 10  | 27 | 9   | 26 |
| 200 | 20 | 190 | 352 | 572 | 1336 | 10  | 26 | 9   | 26 |
| 201 | 20 | 190 | 352 | 572 | 1336 | 10  | 26 | 9   | 26 |
| 202 | 20 | 190 | 352 | 572 | 1336 | 10  | 26 | 9   | 26 |
| 203 | 20 | 190 | 352 | 572 | 1336 | 10  | 26 | 9   | 26 |
| 204 | 20 | 190 | 352 | 572 | 1336 | 10  | 26 | 9   | 26 |
| 205 | 20 | 210 | 389 | 594 | 1207 | 80  | 29 | 79  | 29 |
| 206 | 20 | 210 | 389 | 594 | 1207 | 80  | 29 | 79  | 29 |
| 207 | 20 | 210 | 389 | 594 | 1207 | 80  | 29 | 79  | 29 |
| 208 | 20 | 210 | 389 | 594 | 1207 | 80  | 29 | 79  | 29 |
| 209 | 20 | 210 | 389 | 594 | 1207 | 80  | 29 | 79  | 29 |
| 210 | 20 | 210 | 389 | 594 | 1207 | 80  | 28 | 79  | 29 |
| 211 | 20 | 225 | 417 | 678 | 1060 | 130 | 30 | 129 | 29 |
| 212 | 20 | 225 | 417 | 678 | 1060 | 130 | 30 | 129 | 29 |
| 213 | 20 | 225 | 417 | 678 | 1060 | 130 | 29 | 129 | 29 |
| 214 | 20 | 225 | 417 | 678 | 1060 | 130 | 30 | 129 | 29 |
| 215 | 20 | 225 | 417 | 678 | 1060 | 130 | 29 | 129 | 29 |
| 216 | 20 | 225 | 417 | 678 | 1060 | 130 | 30 | 129 | 29 |